



MEMLS3&a: Microwave Emission Model of Layered Snowpacks adapted to include backscattering

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Abstract. The Microwave Emission Model of Layered Snowpacks (MEMLS) was originally developed for microwave emissions of snowpacks in the frequency range 5–100 GHz. It is based on six-flux theory to describe radiative transfer in snow including absorption, multiple volume scattering, radiation trapping due to internal reflection and a combination of coherent and incoherent superposition of reflections between horizontal layer interfaces. Here we introduce MEMLS3&a, an extension of MEMLS, which includes a backscatter model for active microwave remote sensing of snow. The reflectivity is decomposed into diffuse and specular components. Slight undulations of the snow surface are taken into account. The treatment of like- and cross-polarization is accomplished by an empirical splitting parameter q . MEMLS3&a (as well as MEMLS) is set up in a way that snow input parameters can be derived by objective measurement methods which avoid fitting procedures of the scattering efficiency of snow, required by several other models. For the validation of the model we have used a combination of active and passive measurements from the NoSREx (Nordic Snow Radar Experiment) campaign in Sodankylä, Finland. We find a reasonable agreement between the measurements and simulations, subject to uncertainties in hitherto unmeasured input parameters of the backscatter model. The model is written in Matlab and the code is publicly available for download through the following website: <http://www.iapmw.unibe.ch/research/projects/snowtools/memls.html>.

1 Introduction

Empirical observations reveal a wide range of different microwave signatures in active or passive remote sensing over snow covered areas as shown e.g., by Mätzler (1987). The lack of realistic models to understand these signatures was the motivation for efforts leading to the Microwave Emission Model of Layered Snowpacks (MEMLS) in the 1990s (Mätzler, 1996; Wiesmann and Mätzler, 1999). Initially the microwave emission behavior of single snow layers was investigated by Weise (1996) and later by Wiesmann (1997). The measurements led to an empirical approach for the scattering coefficient of snow in the frequency range 5–100 GHz and correlation-length range 0.05–0.3 mm (Wiesmann et al., 1998) as well as to a first version of MEMLS (Wiesmann and Mätzler, 1999). Empirical relations for the scattering coefficient have also been implemented in the Helsinki University of Technology (HUT) model developed by Pulliainen et al. (1999) and later adapted by Lemmetyinen et al. (2010). MEMLS was extended to coarse-grained snow for correlation lengths up to 0.6 mm (Mätzler and Wiesmann, 1999). The snow microstructure was characterized by an exponential correlation function which allows computing the scattering coefficient analytically using the improved Born approximation (IBA) (Mätzler, 1998).

As an advantage of IBA and the characterization of snow in terms of correlation functions, the most relevant snow input parameters of MEMLS, correlation length and density,

can be measured directly and objectively by various methods. Other models may require e.g., a conversion of measured parameters to model-effective ones (Kontu and Pulliainen, 2010; Lemmetyinen et al., 2015). The exponential correlation length could be e.g., obtained by micro-computed tomography (μ CT) (Schneebeil and Sokratov, 2004) from a fit to the reconstructed three-dimensional microstructure (Löwe et al., 2013). Snow density and correlation length can be also obtained efficiently from field measurements (Proksch et al., 2015) using high-resolution penetrometry (SnowMicroPen – SMP) (Schneebeil and Johnson, 1998). Alternatively, optical methods can be used, e.g., Matzl and Schneebeil (2006); Gallet et al. (2009); Arnaud et al. (2011), to measure the specific surface area (SSA) and use an empirical relation to compute the exponential correlation length (Mätzler, 2002). The latter method is appealing since SSA is commonly available. Accordingly, MEMLS was widely used for various questions related to passive microwave remote sensing (Durand et al., 2008; Rees et al., 2010; Toure et al., 2011; Langlois et al., 2012; Schwank et al., 2014).

In recent years, there was an increasing interest of the snow remote sensing community in active microwave measurements, which was mainly driven by the Cold Regions Hydrology High-Resolution Observatory CoReH₂O (Rott et al., 2010) and related activities. However, single-layer models for the radar signal as presented in Rott et al. (2010) or Ulaby et al. (1984) are mainly used for efficient operation in retrieval schemes. For the sake of low complexity, these models are naturally based on strongly simplifying assumptions, e.g., treating snow as a collection of independent scatterers. However, scatterers are densely packed in snow and strongly interact with each other. More realistic models based on dense media radiative transfer (DMRT) have been developed (Tsang et al., 2007; Chang et al., 2014), including the possibility of using the numerical solution of Maxwell's equations for the single-layer scattering coefficients (Ding et al., 2010; Xu et al., 2012). The DMRT-based models however require at least two microstructural input parameters, which can be presently obtained only by μ CT and often require time consuming casting procedures in the field.

To cope with recent requirements in active microwave remote sensing, while relying on an established, physical model of intermediate complexity, it is the aim of the present paper to extend MEMLS and develop a first version of MEMLS3&a. Thereby, we can build on the description of the microstructure in terms of the exponential correlation length as a single, objective parameter which can be derived from in situ field measurements. For the backscattering model, we shall extend the description of the snowpack in MEMLS to account for a slightly undulated snow surface as shown in Fig. 1. The slightly undulated patches should be small enough to leave the emission largely unaffected but large enough to allow for specular backscattering at near-vertical incidence.

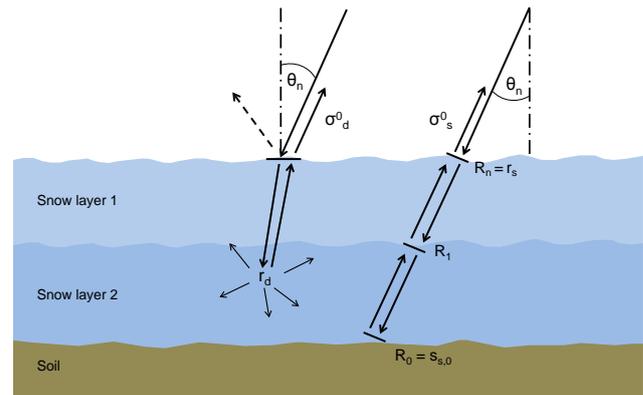


Figure 1. Snowpack (blue) with slightly undulated snow surface and layers. Waves incident at nadir angle θ_n are refracted at the snow surface followed by volume scattering with backscatter σ_d^0 (left). Specular backscatter σ_s^0 from a slightly tilted patch of the surface, soil and layer interfaces (right). Diffuse r_d and specular reflectivities $r_s = R_n$, R_0 and R_1 are indicated.

The paper is organized as follows: in Sect. 2 we present the development of the model and the calculation of the total backscatter with its specular and diffuse components. In Sect. 3 the validation data consisting of active and passive microwave measurements from Sodankylä, Finland, are described. Section 4 presents the validation of both MEMLS and MEMLS3&a using the Sodankylä data, followed by a discussion (Sect. 5) and the conclusions (Sect. 6). Details about the calculation of the specular reflectivity are given in the Appendix.

2 Model development

In MEMLS the snow cover is considered as a stack of n horizontal layers with planar boundaries at the snow surface and between snow layers. Each layer is characterized by snow parameters (layer thickness, correlation length, density, liquid water content and temperature) that determine the layer-radiative properties. Also the salinity can be taken into account layerwise. The snow–ground interface is characterized by a reflectivity s_0 . A sandwich model is used to combine internal scattering and reflections at the interfaces. Internal volume scattering is accounted by a two-flux model (up- and downwelling streams) derived from a six-flux approach (fluxes in all space directions). The absorption and scattering coefficients are functions of the six-flux parameters. The absorption coefficient can be obtained from density, frequency, temperature and salinity; the scattering coefficient depends on the correlation length, density and frequency. For a detailed description of MEMLS we refer to the technical documentation (Mätzler and Wiesmann, 2012). In the following, we focus on the backscatter model by considering the total backscatter as a sum of specular and diffuse components.

Since the total reflectivity of a snowpack is related to its emissivity, it can be derived from passive observations alone. Thereby, active and passive observables can be appropriately combined to obtain a prediction for the radar backscatter.

2.1 Link between active and passive observables

At any given frequency and polarization of electromagnetic radiation with incident direction (μ_n, ϕ_n) defined by zenith angle θ_n (where $\mu_n = \cos\theta_n$) and azimuth angle ϕ_n at the snow–air interface (cf. Fig. 1), the reflectivity r of the surface is related to its emissivity e (in the reciprocal direction) by Kirchhoff’s law:

$$r = 1 - e. \tag{1}$$

For a more general description of Kirchhoff’s law, see Mätzler and Melsheimer (2006). Equation (1) relates the emissivity, the key quantity of passive microwaves, to the reflectivity, a quantity linked to scattering. It is this relation that allows us to link active and passive microwave remote sensing. The reflectivity represents the fraction of the incident radiation that is scattered in the hemisphere above the surface. If the scattered radiation is diffuse (Lambertian reflectance) we can estimate the fraction in the backscatter direction. Furthermore, with information about the statistics of surface slopes, we can determine the contribution of backscatter arising from specular reflection at surface facets that are normal to the incident direction. Therefore, we will represent the total reflectivity as a sum of diffuse and specular components. The reflectivity can be represented as an integral over scattering directions in the upper hemisphere of the bistatic scattering function S :

$$r = \frac{1}{4\pi\mu_n} \int_{2\pi} S(\mu_n, \phi_n, \mu, \phi) d\Omega = \frac{1}{2\mu_n} \int_0^1 S(\mu_n, \mu) . d\mu \tag{2}$$

Here, $d\Omega = d\mu d\phi$ is the infinitesimal solid-angle element in the scattered direction. The azimuth integration extends from 0 to 2π , and the last expression is valid for azimuth-independent functions. The function S describes the scattering from incident direction (μ_n, ϕ_n) to the scattering direction (μ, ϕ) . Thus, backscattering is determined by $S(\mu_n, \phi_n, \mu_n, \phi_n)$. Chandrasekhar (1960) introduced the S function in his monograph on radiative transfer. He showed that S is reciprocal:

$$S(\mu_n, \phi_n, \mu, \phi) = S(\mu, \phi, \mu_n, \phi_n). \tag{3}$$

Furthermore, S is identical to the bistatic scattering cross section σ^0 introduced by Ulaby et al. (1981), see their Eqs. (4.186) and (4.187), more exactly to the sum of the like- and cross-polarization terms, $S = \sigma_{\text{like}}^0(\theta_n, \phi_n, \theta, \phi) + \sigma_{\text{cross}}^0(\theta_n, \phi_n, \theta, \phi)$. It is also related to Peake’s (1959) function $\gamma = S/\mu_n$; i.e., the $1/\mu_n$ factor of Eq. (2) is included inside this function. For completeness, we note that S is related

to but differs from other definitions: the reflection function R used for instance by Kokhanovsky (2001) differs by a factor π from the bidirectional reflection distribution function (BRDF) used in optical remote sensing (Kasten and Raschke, 1974), and all quantities are related by

$$\begin{aligned} S(\mu_n, \phi_n, \mu, \phi) &= \mu_n \gamma(\mu_n, \phi_n, \mu, \phi) \\ &= 4\mu_n \mu R(\mu_n, \phi_n, \mu, \phi) \\ &= 4\pi \mu_n \mu \text{BRDF}(\mu_n, \phi_n, \mu, \phi). \end{aligned} \tag{4}$$

The S function can be highly complex. However, for diffuse scattering, some empirical functions are provided in the literature, see e.g., Mätzler and Rosenkranz (2007), the simplest one for Lambert scattering:

$$S_d = S_0 \mu_n \mu, \tag{5}$$

where the subscript d indicates diffuse scattering, and S_0 is a constant. By integration according to Eq. (2), we find that the diffuse reflectivity r_d is independent of the incidence angle, namely $r_d = S_0/4 = R$, and thus equal to Kokhanovsky’s R . The normalized backscattering cross section is given by $\sigma_d^0 = S_d(\mu = \mu_d)$, which can be expressed by r_d via

$$\sigma_d^0 = 4r_d \mu_n^2. \tag{6}$$

Indeed, Lambertian behavior was found by the investigation of the HPACK model for snow by Mätzler (2000). It is an extension of an earlier one-layer, active–passive model of Tsang et al. (1982) to include multiple-isotropic scattering in the snow as well as refraction and reflection at the snow surface. The combined effect led to Lambert scattering for the diffuse component.

Unspecified in Eq. (6) is the separation of σ_d^0 in its like- and cross-polarized components. For isotropic scatterers considered in HPACK, the first-order backscattering is like-polarized, and cross-polarization requires higher-order scattering. However, the structure of natural snow is highly complex, meaning that cross-polarization occurs for all scattering orders. Therefore, we introduce an empirical relationship with a splitting parameter q which defines the cross-polarized part, whereas $(1 - q)$ represents the like-polarized fraction, via

$$\sigma_{d,pp'}^0 = \begin{cases} (1 - q)\sigma_{d,v}^0, & p = p' = v \\ (1 - q)\sigma_{d,h}^0, & p = p' = h \\ q(\sigma_{d,v}^0 + \sigma_{d,h}^0)/2, & p = v, p' = h \\ & \text{or } p = h, p' = v. \end{cases} \tag{7}$$

Here we took into account that r_d and thus σ_d^0 are slightly different for horizontal (h) and vertical (v) polarization (h- and v-pol). Now, Eq. (6) can be rewritten using the polarization terms for incident waves at vertical and horizontal polariza-

tion, respectively:

$$\begin{aligned}\sigma_{d,v}^0 &= \sigma_{d,vv}^0 + \sigma_{d,hv}^0 = 4r_{d,v}\mu_n^2, \\ \sigma_{d,h}^0 &= \sigma_{d,hh}^0 + \sigma_{d,vh}^0 = 4r_{d,h}\mu_n^2.\end{aligned}\quad (8)$$

An additional contribution to backscattering results from specular reflection as shown in Fig. 1. By considering only slight undulations, specular backscattering is limited to near-vertical incidence. For a Gaussian distribution of surface slopes, the backscattering coefficient of the specular term can be written as

$$\sigma_s^0 = r_{s,0} \frac{\exp[-\tan^2\theta_n/(2m^2)]}{2m^2\mu_n^4}, \quad (9)$$

where m^2 is the mean-square slope, and $r_{s,0}$ refers to r_s at normal incidence (Fig. 1, right). This equation corresponds to the geometrical-optics solution for undulating surfaces, see Ulaby et al. (1982, Eqs. 12.45 and 12.46), and Kong (1986, Sect. 6.6). Here we generalize it from surface scattering to specular terms that fit the observation geometry (i.e., specular reflectivity for local normal incidence angle). Furthermore, we note that Eq. (9) describes like-polarized backscatter. For negligible anisotropy in the local surface plane the same values are obtained for hh (horizontal) and vv (vertical) polarization, and the cross-polarization terms are zero.

For both v and h polarization the total reflectivity is the sum of the diffuse and the specular component:

$$r = r_d + r_s. \quad (10)$$

While Eqs. (6) and (8) are valid for r_d , Eq. (9) applies to r_s but taken at normal incidence. With some additional effort described below, MEMLS provides both r_d and r_s and the total backscattering coefficient as the sum:

$$\sigma^0 = \sigma_d^0 + \sigma_s^0. \quad (11)$$

2.2 Determination of r

Apart from the physical temperatures of all snow layers including the ground temperature, the downwelling sky brightness temperature T_{sky} must also be provided as input in MEMLS. The output is the brightness temperature T_b that is observed as upwelling radiation above the snowpack

$$T_b = rT_{\text{sky}} + (1-r)T_{\text{eff}}. \quad (12)$$

Here T_{eff} is the emission-effective temperature of snow and ground. The reflectivity r can thus be computed via T_b (T_{b1} , T_{b2}) from two arbitrary and different values of T_{sky} ($T_{\text{sky}1}$, $T_{\text{sky}2}$), such as 100 and 0 K. The reflectivity then follows from

$$r = \frac{T_{b1} - T_{b2}}{T_{\text{sky}1} - T_{\text{sky}2}}. \quad (13)$$

2.3 Determination of r_s

According to Fig. 1 we need the specular reflectivities $r_{s,v}$ and $r_{s,h}$ at vertical and horizontal polarization at the observation incidence angle as well as $r_{s,0}$ at normal incidence. For brevity, we omit subscripts indicating the polarization and just write r_s instead of $r_{s,v}$ and $r_{s,h}$. In many situations r_s can be identified by the reflectivity of the snow surface. This is especially true for wet snow and for snowpacks that consist of a single layer. However, if an old snowpack is covered by fresh snow, the dominant specular layer may be the interface between the fresh and the old snow. Also, ice lenses form dominant reflectors inside the snowpack. Therefore, MEMLS requires a method that estimates incoherent specular reflectivities for arbitrary stratifications. This derivation is detailed in the Appendix. As a result, if all layer interfaces are assumed to be smooth and the corresponding interface reflectivities s_j are determined by Fresnel's equations, the specular reflectivity R_j resulting from layers below z_j can be expressed in terms of a recurrence relation

$$R_j = s_j + \frac{[(1-s_j)u_j]^2 R_{j-1}}{1 - u_j^2 s_j R_{j-1}}, \quad j = 1, \dots, n. \quad (14)$$

where s_j is the interface reflectivity on top of layer j and $u_j = \exp(-\gamma_{e,j} d_j / \mu_{j-1})$ is the coherent transmissivity of layer j (Fig. 2). The extinction coefficient is denoted by $\gamma_{e,j}$ and d_j is the layer thickness. The specular reflectivity of the entire snowpack-ground system then is given by

$$r_s = R_n \quad (15)$$

Equation (14) starts with $j = 1$ at the ground as the lowest layer contributing to specular reflection. In contrast to the smooth interfaces assumed between snow layers, the ground is regarded as a rough surface and its reflectivity is additively decomposed into a diffuse and a specular part according to $s_0 = s_{s,0} + s_{d,0}$. Accordingly, the ground reflectivity $R_0 = s_{s,0}$ constitutes the initial condition for the recurrence relation (14).

2.4 Synopsis of the backscatter model

Finally, we briefly recap how specular and diffuse components from the previous section are practically reassembled in MEMLS3&a for the computation of the total backscatter.

1. The total backscatter σ^0 is divided into a specular and diffuse component, σ_s^0 and σ_d^0 , respectively (cf. Eq. 11).
2. The specular component σ_s^0 is derived from Eq. (9) and arises from the rough soil surface (via $s_{s,0}$) and the layer interfaces and the snow-air interface, both of which are assumed to be slightly undulated.
3. The diffuse component of the backscatter σ_d^0 is derived from the diffuse component r_d of the total reflectivity (Eq. 6), which requires the calculation of the total

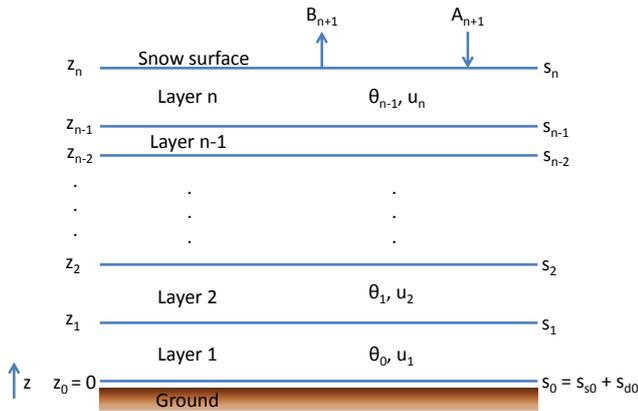


Figure 2. Geometry of the n -layered snowpack with up- and downwelling intensities A and B . Height z_j , transmissivity u_j of directed radiation, refracted angle θ_{j-1} and interface reflectivity s_j for layer number j ranging from 1 (bottom) to n (top). Snow–ground reflectivity s_0 , consisting of the specular s_{s0} and diffuse component s_{d0} .

reflectivity r (Eq. 13) and its specular component r_s (Eqs. 14, 15).

Thus, the model accounts for multiple scattering at the undulated layer interfaces. The diffuse scattered radiation is assumed to be Lambertian, which allows estimating the fraction scattered in the backscatter direction. More complex processes such as coherent backscatter enhancement recently presented by Tan et al. (2015) are currently not considered in MEMLS3&a.

2.5 Primary input parameters

For a simulation run at a given frequency f , polarization p and observation incidence angle θ_n , all snow physical parameters described in Table 1 are required for each snow layer ($j = 1, 2, \dots, n$). From these primary input parameters, secondary parameters are computed as described in the previous version of MEMLS (Wiesmann and Mätzler, 1999).

3 Validation data

We used snow input data generated from three different snow measurement methods to run model simulations which are compared to backscatter measurements from ESA’s SnowScat scatterometer for validation (Werner et al., 2010). All measurements were made on 1 March 2012 at the test site of the Finnish Meteorological Institute (FMI), in Sodankylä, Finland, during ESA’s Nordic Snow and Radar Experiment (NoSREx) III (Lemmetyinen et al., 2013). The snow measurements were conducted directly in the field of view of the scatterometer and the radiometer in order to minimize the influence of the spatial variability of the snowpack.

3.1 Test site

In the NoSREx campaign, the SnowScat scatterometer and SodRad radiometers were installed on two platforms overlooking a forest clearing. For the NoSREx measurements, SnowScat was set to measure several incidence angles over a wide sector. For the purpose of the present work both SnowScat and SodRad were turned in azimuth to point towards the same location on the snowpack, where a destructive snow-pit measurement was made after the microwave measurements were completed.

The soil composition under the snowpack is dominantly mineral soil, with a thin vegetation layer on the surface (ca. 5 cm). A survey conducted in 2010 resulted in a soil composition beneath the vegetation layer of 70 % sand, 1 % clay and 29 % silt. Trees and shrubs higher than 10 cm were removed from the site prior to measurements. The surface vegetation consists of low lichen, moss and heather (Fig. 14).

3.2 SnowScat

The validation data were measured with ESA’s SnowScat instrument (Werner et al., 2010) developed by Gamma remote sensing, Gümmlingen, Switzerland. It is an X-to-Ku band, fully polarimetric step-frequency radar with an internal calibration loop which measures at a frequency range of 9.2–17.8 GHz, with a frequency resolution of 3.072 MHz. Data are presented for three sub-bands with center frequencies of 10.2, 13.3 and 16.7 GHz with 2 GHz bandwidth. The -3 dB beam widths of the horn antennas are 5 and 12° , depending on frequency and polarization. An aluminum sphere is used as calibration target to correct for long-term drifts. The instrument is mounted on a 9 m high tower and is able to rotate in the azimuth direction and to vary the incidence angle. For the validation data used in this study, SnowScat was pointed directly at the location where the in situ measurements were conducted. The instrument was then operated at an incidence angle of 50° .

3.3 SodRad

The SodRad (Sodankylä Radiometer) system was mounted on a 4.1 m high platform. In 2012, measurements at 10.65, 18.7, 21 and 37 GHz (h- and v-pol) were available from the system. The radiometers were calibrated using a two-point calibration with external targets before the start of the campaign. Verification of calibration stability was performed using periodic observations of the sky at zenith. Absolute accuracy of the calibration was estimated to be better than 1 K for the 18.7, 21 and 36.5 GHz channels, and better than 2 K for the 10.65 GHz channel. The beam width of all channels was 6° . The fields of view of the radiometers were clear of all standing vegetation.

Table 1. Primary input parameters used in MEMLS3&a, with snow input parameters for each snow layer (upper part) and general model parameters (lower part). In addition, the value and unit of the parameter, as well as a typical way of determination, are indicated.

| Parameter | Value and unit | Determination |
|--|----------------------------|--|
| density ρ | [0–917] kg m ⁻³ | traditional ^a , SMP, CT |
| exponential correlation length l_{ex} | mm | SMP, CT, (NIP) ^b |
| volume fraction of liquid water | [0–1] | traditional ^a , dielectric ^c |
| snow salinity | [0–0.1] ppt | electric conductivity |
| layer thickness | cm | traditional ^a , SMP, NIP, CT |
| temperature T | K | traditional ^a |
| physical ground temperature T_0 | K | thermometer |
| snow–ground reflectivity s_0 | [0–1] | modeled ^d |
| specular snow–ground reflectivity s_{s0} | [0–1] | estimated from s_0 ^e |
| cross-polarization ratio q | [0–1] | empirical |
| mean slope of surface undulations m | [0–∞] | empirical |

^a Fierz et al. (2009). ^b In combination with a density measurement (Eqs. 16, 17). ^c Denoth et al. (1984). ^d Wegmüller and Mätzler (1999). ^e See text, Sect. 4.1.2.

4 Validation results

4.1 Model initialization

4.1.1 Snow input parameters

The most crucial snow input parameters required to drive MEMLS3&a are density and correlation length. We derived these parameters from three different snow measurement methods in order to illustrate different ways of acquisition (Fig. 3). First, density and correlation length were derived according to Löwe et al. (2011), using three-dimensional reconstruction by μ CT (Schneebeli and Sokratov, 2004) of snow samples cast in the field. The sample casting technique is described in detail by Heggli et al. (2009). Second, we used the SMP (Schneebeli and Johnson, 1998), a high resolution penetrometer. The derivation of density and correlation length from the SMP is detailed in Proksch et al. (2015). Finally, the near-infrared photography (NIP) developed by Matzl and Schneebeli (2006) allows measuring the specific surface area (SSA) of snow which is used to define the length scale:

$$l_c = \frac{4(1 - \rho_{\text{snow}}/\rho_{\text{ice}})}{\text{SSA}}. \quad (16)$$

The exponential correlation length l_{ex} is then obtained from the empirical relation,

$$l_{\text{ex}} = 0.75l_c, \quad (17)$$

put forward by Mätzler (2002).

As NIP does not provide the snow density, it was measured using a standard 100 cm³ density cutter with a vertical sampling interval of 4 cm. A more detailed comparison of snow measurement methods with respect to microwave remote sensing can be found in Proksch and Schneebeli (2012). The density and correlation length profiles derived by the

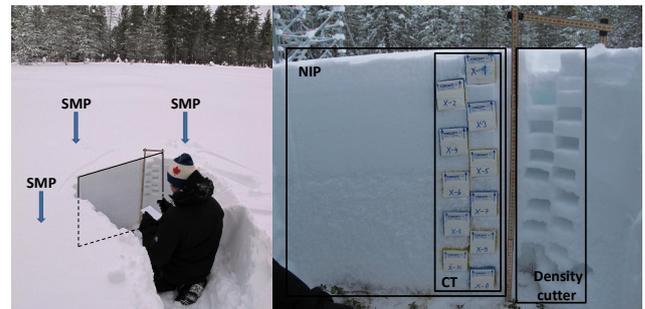


Figure 3. Left: snow-pit overview with the locations of the SnowMicroPen (SMP) measurements (arrows) surrounding the profile wall (black rectangular). Right: close-up of the profile wall, with locations of near infrared photography (NIP), computed tomography (CT) and density cutter measurements.

different methods are shown in Figs. 4 and 5. In general, the different methods are in agreement, besides the correlation length derived from NIP, which shows very large values in the lowest layer, an artifact of the preparation process of the profile wall. The snow temperature was assumed to be constant at -3°C . At this temperature the snow is dry and does not contain liquid water. The density and correlation length profiles were averaged to a vertical resolution of 3 cm to avoid any effects of coherent layers for the wavelength considered by SnowScat.

4.1.2 Soil contribution

Besides the snow input parameters, the snow–ground reflectivity s_0 is required. Since direct measurements were not possible due to the presence of the snow cover, this parameter has to be modeled. Here we used the empirical model of Wegmüller and Mätzler (1999), which was previously used in various studies (e.g., Lemmetyinen et al., 2010;

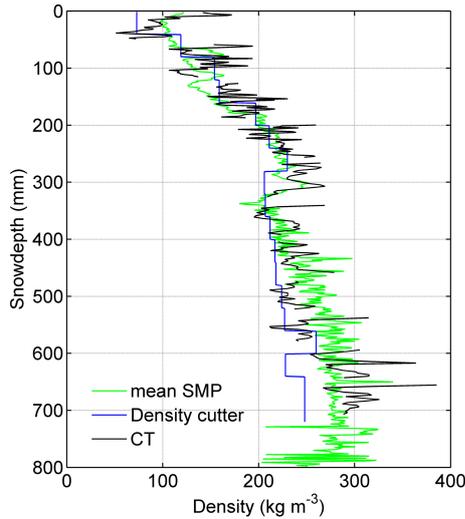


Figure 4. Density profile derived by SMP (green), μ CT (black) and density cutter (blue). The green line is the average of three neighboring SMP measurements.

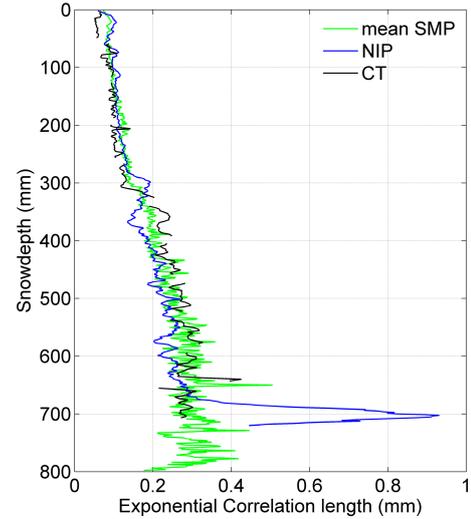


Figure 5. Correlation length profile derived by SMP (green), μ CT (black) and NIP (blue). The blue line is the correlation length derived from the SSA measured by NIP according to Mätzler (2002).

Takala et al., 2011; Rautiainen et al., 2012; Kontu et al., 2014). We used a value for the complex soil permittivity of frozen ground of $\epsilon_g = 3.6 + 0.9i$, in line with Rautiainen et al. (2012), and set the standard deviation of the soil surface height rms_g under the vegetation to 5 mm.

To account for the correct incidence angle at the snow–ground interface, the following auxiliary procedure is carried out for each model run. First, MEMLS3&a is run with $s_0 = 0$ and the incidence angle at the snow–ground interface is determined. Second, this angle was used in the model of Wegmüller and Mätzler (1999) to calculate s_0 which was then used to run MEMLS3&a again, now accounting for the correct incidence angle on the snow–ground interface. The resulting values for s_0 ranged from 0.025 for 18 GHz at v-pol to 0.037 for 10 GHz at h-pol.

The model of Wegmüller and Mätzler (1999) gives the total reflectivity of the snow–ground interface. To determine its specular component s_{s0} , we assumed s_{s0} to be proportional to s_0 . A constant factor of 0.75 ($s_{s0} = 0.75s_0$, for all polarizations and frequencies) was chosen to match SnowScat measurements with our simulations.

The soil temperature was measured to be -2.5°C . For the comparison to SnowScat observations, the cross-polarization fraction q was chosen to match the microwave measurements, which led to $q = 0.15$. The mean slope of surface undulations m has no influence for an incidence angle of 50° if values are smaller than 0.25. We choose $m = 0.1$ for our simulations. The sensitivity to both parameters will be discussed in Sect. 4.2.2.

4.1.3 Sky temperature

A further input to the model is the downwelling brightness temperature T_{sky} of the sky. As SnowScat did not measure T_{sky} , we estimated T_{sky} from the SodRad radiometer which measures the sky brightness temperature $T_{\text{sky},z}$ at zenith. To fit our frequency interval of 10–18 GHz used for the simulation, we linearly interpolated $T_{\text{sky},z}$ values to match the interval. To convert $T_{\text{sky},z}$ to an effective sky brightness temperature T_{sky} , which is representative for the whole scenery at the main test site, we first determined the sky opacity τ_z at zenith from $T_{\text{sky},z}$ (similar to Mätzler, 1994, their Eq. 7):

$$\tau_z = -\ln\left(\frac{T_{\text{sky},z} - T_{\text{air}}}{T_{\text{back}} - T_{\text{air}}}\right), \quad (18)$$

where $T_{\text{air}} = 270\text{ K}$ is the air temperature and $T_{\text{back}} = 2.7\text{ K}$ is the background radiation. A good approximation for the effective opacity (τ_{eff}) representative of the whole scenery is given by

$$\tau_{\text{eff}} = 2\tau_z, \quad (19)$$

as shown by Mätzler (2005). The sky brightness temperature is finally computed from

$$T_{\text{sky}} = 2.7e^{-\tau_{\text{eff}}} + (1 - e^{-\tau_{\text{eff}}})T_{\text{air}}. \quad (20)$$

4.2 Results

4.2.1 Simulation results

We choose the scattering option of the improved Born approximation (Mätzler, 1998) to run the model. For the soil,

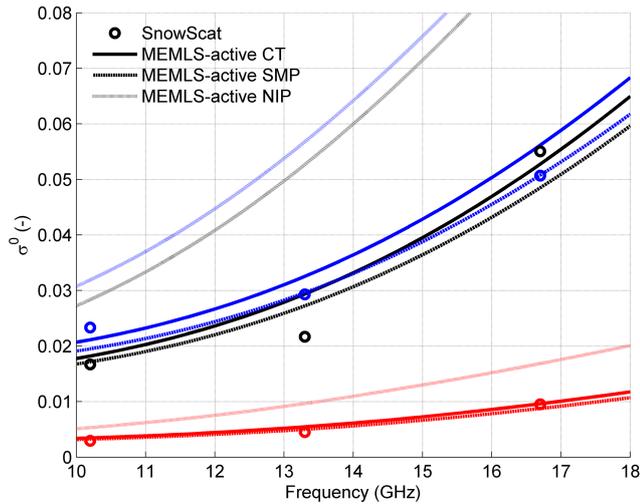


Figure 6. σ^0 measured by SnowScat (circles) and modeled by MEMLS3&a (lines) with SMP (solid), CT (dashed) and NIP (dotted) inputs. MEMLS3&a runs are performed with the snow–ground reflectivity s_0 calculated by Wegmüller and Mätzler (1999), and $s_{s0,h} = 0.75 s_{0,h}$, $s_{s0,v} = 0.75 s_{0,v}$. The mean slope of the surface undulation was set to $m = 0.1$ and the cross-polarization ratio to $q = 0.15$. Colors represent polarization, with vv – black, hh – blue and hv – red.

snow and T_{sky} parameter settings described in Sect. 4.1, the results for MEMLS3&a driven by SMP, CT and NIP input data are shown in Fig. 6 for an incidence angle of 50° . CT and SMP input results in good agreement between model and measurement, with mean absolute errors (MAEs) of 4.0×10^{-3} and 4.3×10^{-3} for vv polarization, 3.2×10^{-3} and 1.6×10^{-3} for hh polarization and 4.0×10^{-4} and 5.3×10^{-4} for hv polarization with CT and SMP inputs, respectively. NIP input leads to an overestimation of σ_0 , which emerges from the NIP artefact towards the bottom of the profile (Sect. 4.1.1) where the correlation length values are too large. However, MEMLS3&a driven with CT input data is in good agreement with SnowScat measurements (Fig. 7).

The dependence on the incidence angle at 10.2 and 16.7 GHz is shown in Figs. 8 and 9. MEMLS3&a is in general agreement with SnowScat, with MAEs of 2.3×10^{-3} and 9.6×10^{-3} for vv polarization, 2.1×10^{-3} and 1.2×10^{-2} for hh polarization and 6.3×10^{-4} and 2.6×10^{-3} for hv polarization at 10.2 and 16.7 GHz, respectively. The polarization difference is slightly too small at 16.7 GHz. The SnowScat observations at different incidence angles show a certain amount of scatter, which we attribute to the heterogeneity of the ground and snow cover at the test site.

4.2.2 Sensitivity analysis

In this section, the sensitivity of MEMLS3&a to s_{s0} as well as to the two empirical parameters, the cross-polarization ratio q and the root-mean-square slope of surface undula-

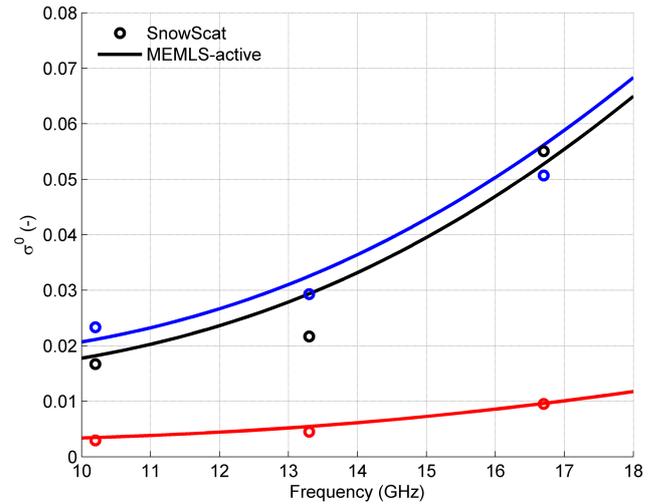


Figure 7. σ^0 at incidence angle 50° measured by SnowScat (circles) and modeled by MEMLS3&a with CT input (lines) for best fit parameters: $s_{s0,h} = 0.75 \cdot s_{0,h}$; $s_{s0,v} = 0.75 \cdot s_{0,v}$; $q = 0.15$; and $m = 0.1$. Colors represent polarization, with vv – black, hh – blue and hv – red.

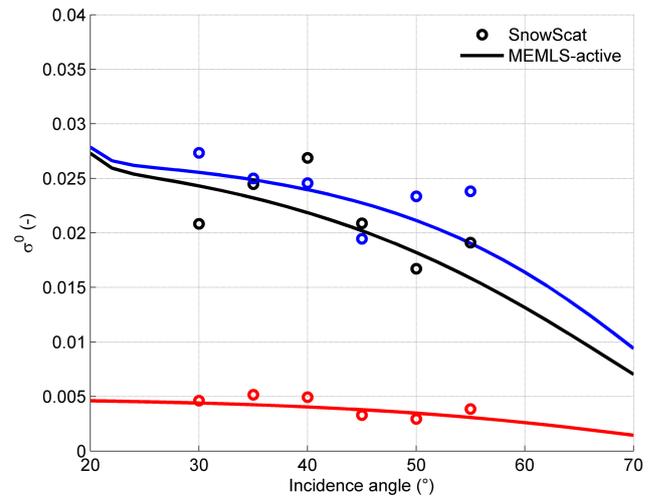


Figure 8. σ^0 at 10.2 GHz measured by SnowScat (circles) and modeled by MEMLS3&a with CT input (lines). Colors represent polarization, with vv – black, hh – blue and hv – red. Best fit parameters according to Fig. 7.

tions m , are shown. For clarity, we restrict ourselves to those MEMLS3&a runs which were driven with CT input data and the best fit values mentioned above ($q = 0.15$, $m = 0.1$, and $s_{s0} = 0.75 s_0$ for both polarizations), if not indicated differently.

The specular snow–ground reflectivity s_{s0} is a crucial parameter for the simulation because a higher specular snow–ground reflectivity leads to lower backscatter. This effect is larger at low frequencies due to the lower attenuation of electromagnetic radiation in snow. Figure 10 shows that σ^0 is

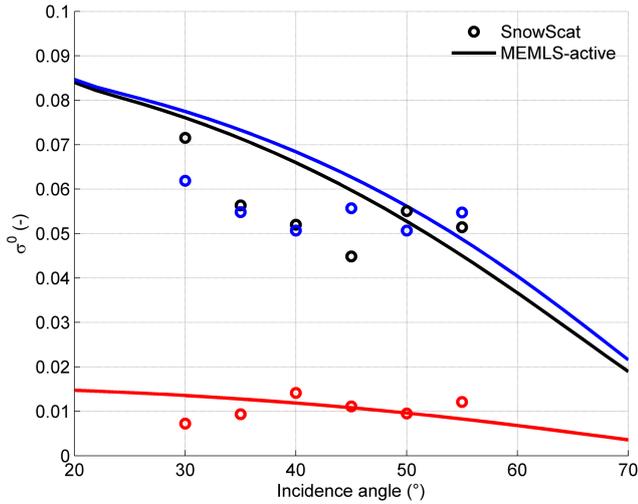


Figure 9. σ^0 at 16.7 GHz measured by SnowScat (circles) and modeled by MEMLS3&a with CT input (lines). Colors represent polarization, with vv – black, hh – blue and hv – red. Best fit parameters according to Fig. 7.

significantly increased with decreasing s_{s0} values and vice versa, more pronounced at low frequencies.

The empirical cross-polarization ratio q is the fraction of cross-polarized backscatter: increasing q lowers co-polarization and increases cross-polarization by the same magnitude (cf. Eq. 7). Figure 11 illustrates this by two values of q (0.15 and 0.3, respectively).

A larger value of m represents a stronger undulated surface and increases the spectral component of the backscatter, in particular at small incidence angles. Figure 12 shows this behavior, with increasing backscatter for increasing values of m and decreasing incidence angles. Given values smaller than 0.1, m has no effect at incidence angles larger than 25° . Furthermore, cross-polarization is in general not affected by m . Note that these results are only valid for the given snow and soil conditions, i.e., the sensitivity of parameters might change in different environmental conditions.

4.2.3 Comparison with passive simulations

To prove the concept of the MEMLS architecture, which is the fundament for MEMLS3&a, we compare our active simulations with passive simulations using the same input data (Sect. 4.1). The validation data were measured by the SodRad radiometer (Sect. 4.1.3). Similar to SnowScat, SodRad was also pointed to the location of the in situ measurements (azimuth angle 140°). The instrument was operated at an incidence angle of 50° .

To run MEMLS, 15 SMP measurements inside the main test site in Sodankylä were used in order to capture the spatial variability of the snowpack. For each SMP measurement one MEMLS simulation was conducted. Figure 13 shows the

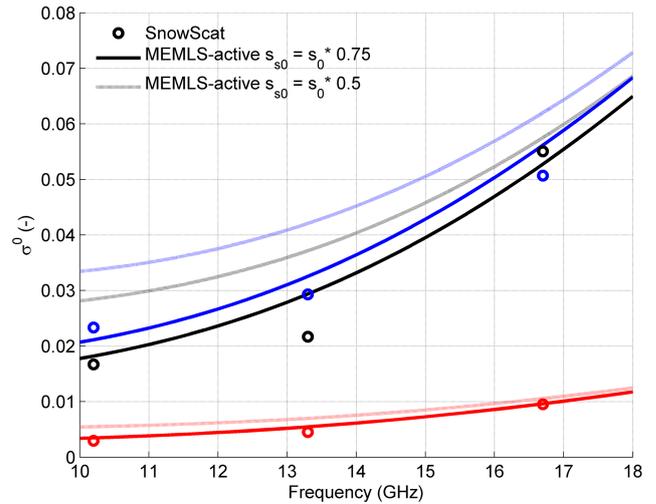


Figure 10. σ^0 at incidence angle 50° measured by SnowScat (circles) and modeled by MEMLS3&a with CT input (lines) for different specular snow–ground reflectivities s_{s0} . Higher s_{s0} values lead to lower σ^0 values and vice versa. Colors represent polarization, with vv – black, hh – blue and hv – red. Best fit parameters according to Fig. 7.

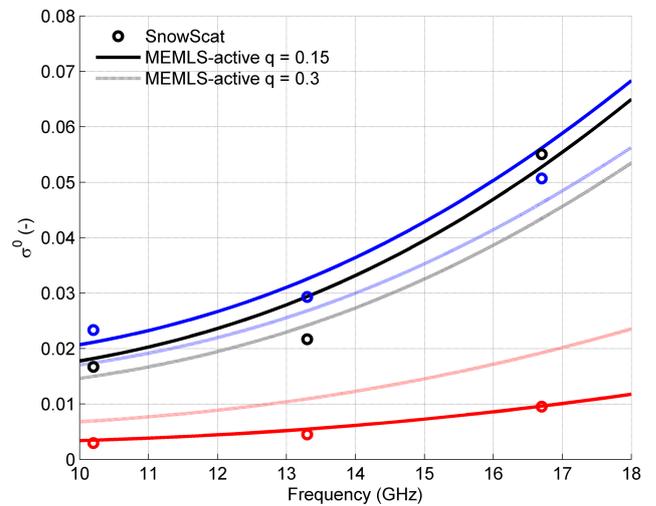


Figure 11. σ^0 at incidence angle 50° measured by SnowScat (circles) and modeled by MEMLS3&a with CT input (lines) for different cross-polarization ratios q . Higher q ratios lead to lower σ^0 values for co-polarization and higher σ^0 values for cross-polarization. Colors represent polarization, with vv – black, hh – blue and hv – red. Best fit parameters according to Fig. 7.

results of the 15 MEMLS runs in combination with the SodRad measurements.

The agreement between model and observation generally decreased towards higher frequencies. At 36 GHz the average of all 15 MEMLS runs was at maximum 22 K too low for v-pol and 12 K too low for h-pol. Compared to the operational azimuth angle of 190° , the difference between model and ob-

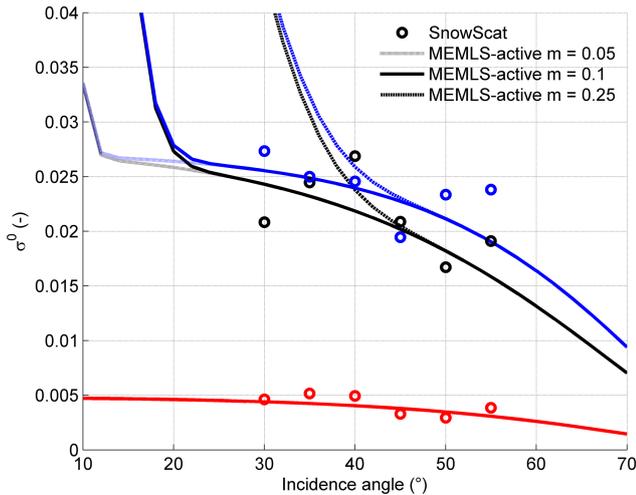


Figure 12. σ^0 measured by SnowScat (circles) and modeled by MEMLS3&a with CT input (lines) at 10.65 GHz for different mean slope of surface undulations m . Colors represent polarization, with vv – black, hh – blue and hv – red. Best fit parameters according to Fig. 7.

servation decreased to 16 and 1 K for v-pol and h-pol, respectively. The differences at 10 GHz are comparably lower, with 5 K at maximum. The standard deviations of the 15 MEMLS runs, which are solely due to spatial variability of the snow, increased with frequency. At 36 GHz, the standard deviation was around 8 K for both polarizations. The difference in azimuth angles of SodRad was even larger, with 12 K at 36 GHz h-pol. This underlines the influence of the spatial variability of the snowpack on modeled and measured brightness temperatures, which will be discussed in the next section. The agreement between model and observation should be always interpreted with respect to the variation in brightness temperatures caused by the spatial variability of the snowpack.

5 Discussion

As shown in Sect. 4, MEMLS3&a simulations were in reasonable agreement with SnowScat observations. To achieve this agreement, however, several parameters were chosen to match model and observation. This was necessary, since the active part contains, in contrast to the passive part, empirical parameters (s_{s0} , q and m) which could not be measured. Likewise, the ground parameters s_0 and rms_g are subject to uncertainties.

The specular part of the snow–ground reflectivity s_{s0} was chosen to be proportional to s_0 and the same factor of 0.75 could be applied for all frequencies and polarizations to convert s_0 into s_{s0} . With $s_{s0} = 0.75s_0$, the main part of the snow–ground reflectivity is specular. This requires the ground to be smooth and the overlaying snow layer to be transparent. The vegetation is subject to very low temperatures and a steady

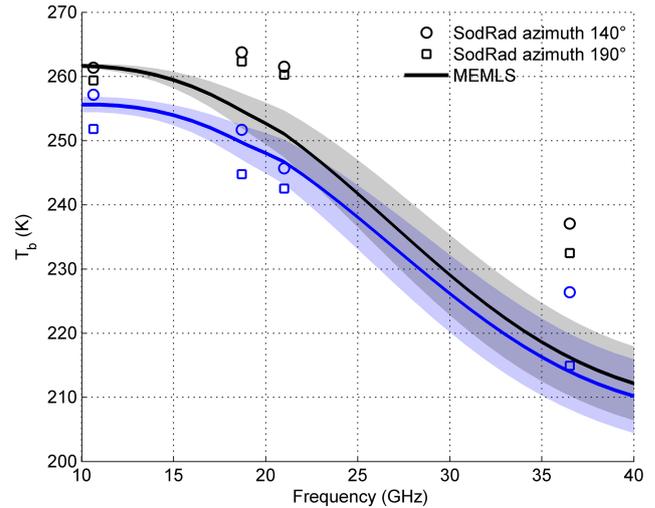


Figure 13. T_b measured by SodRad at an azimuth angles of 190° (circles) and at 140° (squares). T_b modeled by MEMLS from 15 SMP measurements, average (lines) with standard deviation (shaded). Colors represent polarization, with v – black and h – blue.

temperature gradient, which forces the water of the soft vegetation (lichen, mosses, shrubs (myrtillus species); Fig. 14) to move upwards into the snow. Given the height of the vegetation of less than 10 cm, it seems reasonable to assume that the vegetation dries out during winter and can be treated as fully transparent for the present microwave frequencies. This allows the soil interface to act as specular reflector, which is then accounted for by s_{s0} in the model. Though being reasonable, a sound justification of this line of argumentation requires further investigations.

The cross-polarization in MEMLS3&a is solely determined empirically via the parameter q . This pragmatic approach was chosen since the physical origin of cross-polarization in snow is still the subject of ongoing research. In the DMRT based approach (Tsang et al., 2007), cross-polarization emerges from non-spherical shapes of aggregated sphere clusters. A different route to cross-polarization can be taken via the discrete dipole approximation (DDA), e.g., from Von Lerber et al. (2006) or Xu et al. (2012), which principally accounts for multiple reflections and polarizations inside a given snow volume. DDA requires the full three-dimensional description of the microstructure, which can be provided by μCT . A comparison to such a model could further elucidate the justification and the value of the parameter q .

Another parameter chosen empirically is the mean slope of surface undulations m . In principle, this parameter could be obtained from the analysis of the surface height, similar to what has been done in Löwe et al. (2007) and Manes et al. (2008) for fresh snow. In a simple reasoning, the mean squared slope m can be expressed as the ratio between the standard deviation of the surface height and the lateral cor-



Figure 14. View of about 1 m^2 of the snow-free surface at the radiometer test site in Sodankylä, Finland.

relation length of the height correlation function. According to Manes et al. (2008) m would then take a value of 0.14 for fresh snow which is in the same order of magnitude as applied in our simulations ($m = 0.1$). This small-scale roughness of the snow surface is not taken into account by the model, where only slight surface undulations are allowed.

The individual magnitudes of the specular and diffuse contributions are shown in Fig. 15. Towards higher frequencies, the diffuse component increases and outweighs the specular reflectivity from 12.5 GHz for v-pol and from 14.5 GHz for h-pol. Note that the magnitude of the specular component also depends on the undulation of the surface and therefore on the value of m . However, a pronounced impact of m is limited to small incidence angles (Fig. 12 and Sect. 4.2.2) for reasonable values of m ($m \approx 0.1$).

In contrast to MEMLS3&a, MEMLS does not require free empirical parameters. In this regard, we attribute the fact that MEMLS3&a matches the SnowScat observation better than MEMLS the SodRad observations to the additional free parameters in MEMLS3&a, foremost s_{s0} and q . However, for the passive simulations, parameters also had to be chosen without direct experimental justification, namely s_0 and rms_g , which determine the contribution of the snow–ground interface. This contribution is dominant and critical in our frequency range, as dry snowpacks thinner than $\sim 1\text{ m}$ are highly transparent. Unfortunately, the knowledge about the scattering at the ground surface is limited. Therefore, the snow–ground reflectivity s_0 was modeled using the model of Wegmüller and Mätzler (1999). This model is an empirical parametrization of the Fresnel formula depending on the standard deviation of the soil surface height rms_g and the soil permittivities. For the soil permittivities, Hallikainen et al. (1985) provide experimental data and Mironov et al. (2010) an empirical model based on experimental data, but dielectric models for the permittivities of frozen soils are still under development. For rms_g of the soil below the snowpack no measurements were available. In addition, the model of

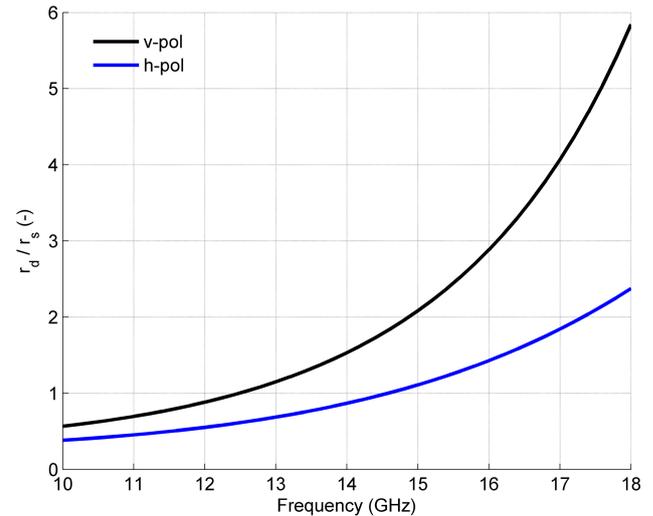


Figure 15. Ratio of the simulated diffuse (r_d) and specular (r_s) reflectivity at 50° incidence angle per frequency, for the best fit parameters according to Fig. 7.

Wegmüller and Mätzler (1999) does not account for vegetation, which is in our case consistent with the argument on transparency given above. We note that estimating the snow–ground reflectivity is critical for all microwave models, which was also concluded from recent experiments (Roy et al., 2013; Montpetit et al., 2013). However, at 10 GHz, the frequency which is most influenced by the soil; MEMLS and SodRad were in good agreement.

In contrast, the mismatch between model and measurements was largest at 36 GHz and is most sensitive to details of the snow microstructure. MEMLS assumes an exponential fit of the density correlation function of the snow microstructure. The exponential fit is a reasonable starting point but small deviations can have a large influence on scattering. As detailed by Löwe et al. (2011), the correlation function of snow can take different shapes and its representation by means of a single correlation length might be inappropriate. Instead the Teubner–Strey form, a two-scale form for bicontinuous media might be more appropriate. The inclusion of other types of correlation functions into MEMLS is possible by adapting the calculation of the scattering coefficient. We thus believe that the present model provides a suitable test case to investigate the impact of more sophisticated representations of the snow microstructure.

We further tried to assess the influence of the spatial variability of the snowpack. The standard deviation obtained from the 15 MEMLS runs is 8 K at 36.5 GHz, h- and v-pol, implying a non-negligible influence of the location of the in situ snow measurements on the modeled brightness temperatures.

We also found that the higher values measured by SodRad throughout the whole frequency range at h-pol for an azimuth angle of 140° indicate an effect of the surrounding environ-

ment, such as trees, which were closer to the field of view at this azimuth angle. The spatial variability of the snowpack together with the influence of the environment is potentially able to bias simulated and measured brightness temperatures.

The degree of complexity of existing models simulating microwave backscattering from snow range from single-layer approaches (Rott et al., 2010) to numerical solutions of Maxwell's equations (Xu et al., 2012; Ding et al., 2010). In this context, we propose MEMLS3&a as a model of intermediate complexity. In contrast to the HUT model (Pulliainen et al., 1999; Lemmetyinen et al., 2010), which has comparable complexity, MEMLS avoids traditional grain size as input parameter, which is prone to uncertainties in the visual estimation method (Painter et al., 2007). The advantage of MEMLS3&a (as well as MEMLS) is the correlation length as microstructural quantity, which can be obtained from objective measurements without conversion and, given the SMP retrieval method, with high efficiency in the field.

Presently, models differ not only in the representation of snow microstructure but also in the solution of the radiative transfer or the type of interfaces between the layers, which makes it difficult to attribute the discrepancies in model performance to a particular part of the model. A comparison by Tedesco and Kim (2006) of at least the passive models showed that no model was able to reproduce all of the investigated microwave observations. For a detailed model assessment in view of future developments, various effects (spatial variability, snow microstructure, soil) must be isolated. A promising way is by using measurements of specifically prepared snow slabs, as already presented by Wiesmann et al. (1998). Together with complete 3-D microstructural information, these types of idealized experiments will allow us to

minimize spatial variability, avoid the influence of the ground and compare different microstructural concepts for scattering coefficients. Together with available multi-layer models like MEMLS3&a, DMRT-ML (Picard et al., 2013) or the DMRT-QMS package (Chang et al., 2014), this will clarify our understanding of the processes involved in microwave emission and scattering of snow.

6 Conclusions

We adapted the MEMLS to include backscattering and presented a detailed description of the relevant parameters and their derivation. The reflectivity was decomposed into diffuse and specular components, and the snowpack was allowed to be slightly undulated. This procedure could be applied to other passive microwave models as well. Model simulations were in reasonable agreement with scatterometer observations, if the specular snow-ground reflectivity s_{s0} and the cross-polarization ratio q were chosen accordingly. We found that the contribution of the snow-ground interface is a critical parameter, which needs further investigation. The empirical formulation of the cross-polarization ratio q is a limitation with respect to other existing microwave models. MEMLS3&a is a model of intermediate complexity, which avoids fitting procedures of the scattering efficiency of snow in combination with SMP or μ CT measurements. This eliminates a main uncertainty of snow characterization in microwave remote sensing.

MEMLS3&a is integrated in the standard release of MEMLS as a separate sub-routine. Both versions, active and passive are built on the same set of core functions.

Appendix A: Specular reflectivity of the layered snowpack

The purpose of the appendix is to derive the specular part of the reflectivity of a layered snowpack, in order to separate it from the diffuse part by subtraction from the total reflectivity using MEMLS. It is assumed here that all layer interfaces are smooth and parallel to the surface in order to produce specular reflection. Separation between diffuse and specular reflection is required in bistatic scattering and in backscatter models.

We consider a plane-parallel snowpack used in MEMLS as shown in Fig. 2. The relevant quantities of an arbitrary layer j are shown in detail in Fig. A1. The layer is specified by a transmissivity u_j for the directed radiation. The transmissivity is given by

$$u_j = \exp(-\gamma_{e,j}d_j/\cos\theta_{j-1}), \quad (\text{A1})$$

where $d_j = z_j - z_{j-1}$ is the thickness and $\gamma_{e,j}$ is the extinction coefficient of layer j , respectively. In addition, the layer interfaces are characterized by an interface reflectivity, where s_j denotes the reflectivity of the top interface of layer j . Assuming smooth interfaces, we can apply the Fresnel formulas to compute s_j . The propagation angle θ_{j-1} in layer j is given by Snell's law of refraction. At the bottom of the snowpack, the reflectivity $s_0 = s_{s0} + s_{d0}$ consists of a specular s_{s0} and a diffuse s_{d0} component.

The aim of the following procedure is to derive an expression for the total specular reflectivity, R_j , which results from transmission and reflections in all layers below z_j . In order to compute the specular reflectivity we assume sufficiently large directional intensities such that thermal radiation can be neglected. Note that A_j , B_j , C_j and D_j are downwelling and upwelling intensities just above and below the boundaries of the respective snow layer. By virtue of Fig. A1 we can derive the following equations relating the directional intensities at the boundaries:

$$A_j = u_j C_j, \quad (\text{A2})$$

$$B_j = R_{j-1} A_j, \quad (\text{A3})$$

$$C_j = (1 - s_j) A_{j+1} + s_j D_j, \quad (\text{A4})$$

$$D_j = u_j B_j, \quad (\text{A5})$$

$$B_{j+1} = R_j A_{j+1} = (1 - s_j) D_j + s_j A_{j+1}. \quad (\text{A6})$$

Furthermore, at the bottom we have

$$R_0 = s_{s0}, \quad (\text{A7})$$

where s_{s0} is the specular part of the ground-snow interface reflectivity.

In order to solve these equations for R_j , we first eliminate the D_j and C_j in Eqs. (A4) and (A6) by using Eqs. (A2) and (A5). In this way we obtain

$$u_j(1 - s_j)A_{j+1} = A_j - u_j^2 s_j B_j, \quad (\text{A8})$$

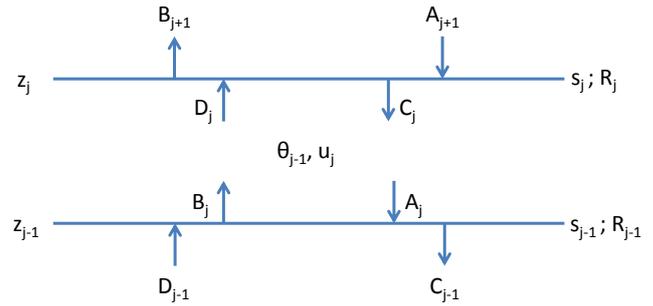


Figure A1. The parameters of a selected layer j : height z_j , up- and downwelling intensities A , B , C , and D ; transmissivity u_j of directed radiation; refracted angle θ_{j-1} ; interface reflectivity s_j ; and specular reflectivity R_j .

and

$$B_{j+1} = (1 - s_j)u_j B_j + s_j A_{j+1}. \quad (\text{A9})$$

Dividing Eq. (A8) by A_j and Eq. (A9) by A_{j+1} we get, together with Eqs. (A6) and (A3),

$$u_j(1 - s_j)A_{j+1}/A_j = 1 - u_j^2 s_j R_{j-1}, \quad (\text{A10})$$

and

$$R_j = (1 - s_j)u_j R_{j-1} A_j/A_{j+1} + s_j. \quad (\text{A11})$$

Eliminating the ratio $A_{j+1}/A_j = (1 - u_j^2 s_j R_{j-1})/[u_j(1 - s_j)]$ in Eq. (A11) leads to

$$R_j = s_j + [(1 - s_j)u_j]^2 R_{j-1} / (1 - u_j^2 s_j R_{j-1}). \quad (\text{A12})$$

Equation (A12) is a recurrence relation for the total specular reflectivity at the snow surface, $r_s = R_n$. The initial condition for the recurrence relation is given by the ground reflectivity in Eq. (A7).

The described procedure is applied for horizontal and vertical polarization, separately. For v polarization we call $R_n = r_{s,v}$, and for h polarization we call $R_n = r_{s,h}$. These are the specular parts of the total reflectivities, r_v and r_h of MEMLS. The diffuse components $r_{d,v}$ and $r_{d,h}$ are thus

$$\begin{aligned} r_{d,v} &= r_v - r_{s,v}, \\ r_{d,h} &= r_h - r_{s,h}. \end{aligned} \quad (\text{A13})$$

The diffuse components should be nearly the same at both polarizations. This property can be tested by computing $r_{d,v}$ and $r_{d,h}$ from Eqs. (10) and (13), taking the total reflectivities from MEMLS and the specular reflectivities from the method described here.

Code availability

The model is written in Matlab and available to the public through the following website: <http://www.iapmw.unibe.ch/research/projects/snowtools/memls.html>.

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