TempestExtremes: a framework for scale-insensitive pointwise feature tracking on unstructured grids

Paul A. Ullrich1 and Colin M. Zarzycki2

1Department of Land, Air and Water Resources, University of California, Davis, One Shields Ave., Davis, CA 95616, USA
2National Center for Atmospheric Research, Boulder, CO, USA

Correspondence to: Paul A. Ullrich (paullrich@ucdavis.edu)

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Abstract. This paper describes a new open-source software framework for automated pointwise feature tracking that is applicable to a wide array of climate datasets using either structured or unstructured grids. Common climatological pointwise features include tropical cyclones, extratropical cyclones and tropical easterly waves. To enable support for a wide array of detection schemes, a suite of algorithmic kernels have been developed that capture the core functionality of algorithmic tracking routines throughout the literature. A review of efforts related to pointwise feature tracking from the past 3 decades is included. Selected results using both reanalysis datasets and unstructured grid simulations are provided.

1 Introduction

Automated pointwise feature tracking is an algorithmic technique for objective identification and tracking of meteorological features, such as extratropical cyclones, tropical cyclones and tropical easterly waves, and has emerged as an important and desirable data processing capability in climate science. Software tools for feature tracking – typically referred to as “trackers” – have been employed to evaluate model performance and answer pressing scientific questions regarding anticipated changes in atmospheric features under climate change. Exploration of tracker literature has exposed a breadth of potential techniques that have been applied to climate datasets with varied spatial resolution and temporal frequency (a comprehensive review of the tracking literature can be found in Appendices A, B and C). Nonetheless, the definition of an optimal objective criteria for key atmospheric features has eluded development, and ambiguity in the formal definition of these features suggests that there may be no singular criteria capable of both perfect detection and zero false alarm rate. Further, as observed by Walsh et al. (2007) and Horn et al. (2014) for tropical cyclones and Neu et al. (2013) for extratropical cyclones, feature tracking schemes can produce wildly varying results depending on the specific choice of threshold variables and values. Therefore, we argue that uncertainties associated with objective tracking criteria should be addressed with an ensemble of detection thresholds and variables, whereas blind application of singular tracking formulations should be avoided. To this end, it is the goal of this paper to review the vast literature on trackers and use this information to inform the development of a unified framework (TempestExtremes) that enables a variety of tracking procedures to be quickly and easily applied across arbitrary spatial resolution and temporal frequency. This paper focuses largely on the technical aspects of pointwise feature tracking, but sets the stage for future studies on parameter sensitivity and optimization.

Most algorithmic Lagrangian trackers of pointwise features (such as cyclones and eddies) share a common procedure:

1. They must identify an initial set of candidate points by searching for local extrema. Local extrema can be further specified, for instance, by requiring that they be sufficiently anomalous when contrasted with their neighbors. For most cyclonic structures, either minima in the sea level pressure field or maxima in the absolute value of the relative vorticity are used.
2. They must eliminate candidate points that do not satisfy a prescribed set of thresholds. For instance, tropical cyclones typically require the presence of an upper-level warm core that is sufficiently near the sea level pressure minima that defines the storm center. Additional criteria, such as a minimum threshold on relative vorticity, can be used to eliminate spurious detections.

3. They must connect candidate points together in time (referred to as “stitching”) to generate feature paths, eliminating paths that are of insufficient length or do not meet additional criteria.

Although the actual implementations of this procedure does vary throughout the literature, a review of this material reveals several core algorithms (kernels) that are common across implementations. Based on our analysis, the five most commonly employed kernels are

- computation of anomalies in a data field from a spatially averaged mean;
- identification of local extrema in a given 2-D data field (for instance, sea level pressure minima);
- determination of whether a closed contour exists in a data field around a particular point;
- determination of whether, in the neighborhood of a particular point, a data field satisfies a given threshold; and
- stitching of candidates from sequential time slices to build feature tracks.

The development of a robust implementation of these five kernels will be the focus of the remainder of this paper.

Feature tracking that is robust across essentially arbitrary datasets requires some additional considerations. Detection criteria and thresholds for tracking are often tuned based on the characteristics of a particular dataset, such as temporal resolution, spatial resolution and regional coverage. Unfortunately, this has led to an abundance of schemes that often cannot be directly compared, or applied in a more general context. To this end, we focus on kernels that are insensitive to the characteristics of the input data. For instance, averaging or searching over a discrete number of grid points around each candidate (a common approach) is incompatible with scale insensitivity since the physical search radius would be dependent on the spatial resolution of the data. Identification of local extrema is also a resolution-sensitive procedure, since the number of extrema will often scale with the number of spatial data points; however, a closed contour criteria based on a physical distance is largely resolution insensitive. To achieve robust applicability, a general framework should

- support structured and unstructured grids (this eliminates the need for post-processing of large native grid output files and enables detection and characterization simultaneous with the model execution);
- not contain hard-coded variable names, so as to ensure robust applicability across reanalysis datasets and applicability to a variety of problems; and
- allow for easy intercomparison of detection schemes by enabling detection criteria and thresholds that are compactly specified on the command line.

Well-known automated software trackers include TRACK (Hodges, 1994, 1995, 2015) and the Geophysical Fluid Dynamics Laboratory (GFDL) TSTORMS package (Vitart et al., 1997; Zhao et al., 2009). Both of these software packages have been used extensively to examine pointwise features in the atmosphere, but do not completely satisfy the four requirements above.

The remainder of the paper is organized as follows: Sect. 2 describes the algorithms and kernels that have been implemented in the TempestExtremes software framework. Selected examples of tropical cyclone, extratropical cyclone and tropical easterly wave detection are then provided in Sect. 3, followed by conclusions in Sect. 4. The appendices provide a review of relevant literature on pointwise feature trackers of extratropical cyclones (Appendix A), tropical cyclones (Appendix B) and tropical easterly waves (Appendix C). A technical guide to the use of the TempestExtremes tools DetectCyclonesUnstructured and StitchNodes is provided in Appendices D and E. Additional examples and updates are available as part of the software package.

2 TempestExtremes algorithms and kernels

This section describes the key building blocks that have been developed in constructing our detection and characterization framework. Pseudocode is utilized throughout to describe the structure of each algorithm.

2.1 Unstructured grid specification

For purposes of determining connectivity of the unstructured grid, we require the specification of a node graph that enumerates the neighbors of each node (one such node graph is depicted in Fig. 1). The connectivity information is stored textually as an adjacency list via a variable-length comma-separated variable file. The total number of nodes \( N \) is specified at the top of the file, followed by \( N \) lines containing the longitude (lon), latitude (lat), associated area, number of adjacent nodes and finally a 1-indexed list of all adjacent nodes, such as depicted below:
Great-circle distance

As mentioned earlier, in order to avoid sensitivity of the detection scheme to grid resolution, great-circle distance has been employed throughout. In terms of regular latitude–longitude coordinates, the great-circle distance \( r \), for a sphere of radius \( a \), between points \((\lambda_1, \phi_1)\) and \((\lambda_2, \phi_2)\), is defined via the symmetric operation:

\[
r(\lambda_1, \phi_1; \lambda_2, \phi_2) = a \arccos \left( \sin \phi_1 \sin \phi_2 + \cos \phi_1 \cos \phi_2 \cos(\lambda_1 - \lambda_2) \right).
\]

Algorithmically, this calculation is implemented as \( \text{gcdist}(p, q) \) for given graph nodes \( p \) and \( q \). The difference between great-circle distance and latitude–longitude distance is striking at high latitudes, as depicted in Fig. 2. Whereas latitude–longitude distance is generally sufficient for tropical cyclone detection, tracking of high-latitude phenomena such as extratropical cyclones is expected to be more consistent when great-circle distance is employed.

Efficient neighbor search using k-d trees

Three-dimensional \((k = 3)\) k-d trees (Bentley, 1975) are used throughout our detection code using the implementation of Tsombikas (2015). k-d trees are a data structure that enable \( O(\log N) \) average time for nearest neighbor search, where \( N \) is the total number of nodes, while also requiring only \( O(N \log N) \) construction time and a \( O(N) \) data storage requirement. Although k-d trees use 3-D straight-line distance instead of great-circle distance, we utilize the observation that straight-line and great-circle distance maintain the same ordering for points confined to the surface of the sphere.

An example k-d tree in two dimensions is depicted in Fig. 3, along with a brief description of how the nearest-neighbor algorithm is performed.

Computing a spatially averaged mean

Many existing tracking algorithms use either a spatially averaged mean field (over a given distance) or an anomaly field computed against the spatially averaged mean (Haarsma et al., 1993; Bengtsson et al., 1995). The mean operation (implemented in TempestExtremes as \( \_\text{MEAN}() \) in the variable specification) is computed on unstructured grids via graph search (see Algorithm 1). Anomalies from the mean can then be computed in conjunction with the \( \_\text{DIFF} \) operator (see Appendix D1).
Algorithm 1: Compute the spatial mean value of a field G over a region of radius dist using graph search on an unstructured grid.

```
field F = mean(field G, dist)
for each node p
    total_area = 0
    F[p] = 0
    visited = []
tovisit = [p]
while tovisit is not empty
    q = remove node from tovisit
    add q to visited
    total_area = total_area + area[q]
    for each neighbor s of q
        if (gcd(p,s) < dist) and
            (s is not in visited) then
            add s to tovisit
```

2.5 Extrema detection

For purposes of computational efficiency, candidate points are initially located by identifying local extrema in a given field (for instance, sea level pressure (SLP)) via find_all_minima (Algorithm 2). This algorithm compares all nodes against their associated neighbors and only tags points that are less/greater than those neighbors. Candidates are then eliminated if they are “too close” to stronger extrema (Algorithm 3) (e.g., Pinto et al., 2005). This algorithm is performed by eliminating candidate nodes that are within a given distance of a stronger extrema. The initial search field is specified to TempestExtremes either via the --searchbymin or --searchbymax command line argument. The merge distance used in merge_candidates_minima is specified via the --mergedist command line argument.

Algorithm 2: Locate the set of all nodes P that are local minima for a field G (for instance, SLP) defined on an unstructured grid. The procedure for locating maxima is analogous.

```
set P = find_all_minima(field G)
for each node f
    is_minima[f] = true
    for each neighbor node v of f
        if G[v] < G[f] then
            is_minima[f] = false
    if is_minima[f] then
        insert f into P
```

Algorithm 3: Given a field G defined on an unstructured grid and a set of candidate points P, remove candidate minima that are within a distance dist of a more extreme minimum, and return the new candidate set Q.

```
set Q =
merge_candidates_minima(field G, set P, dist)
K = build_kd_tree(P)
for each candidate p in P
    retain_p = true
    N = kd_tree_all_neighbors(K, p, dist)
    for all q in N
        if (G[q] < G[p]) then
            retain_p = false
        if retain_p then insert p into Q
```

2.6 Closed contour criteria

Although a first pass at candidate points may be made by looking for local extrema (comparing against all neighboring nodes), this criteria is not robust across model resolutions. That is, the distance between a node and its neighbors decreases proportionally to the local grid spacing, and so does not define a “physical” criterion. Consequently, we instead advocate for a “closed contour criteria” to define candidate nodes. Closed contours were first employed by Bell and Bosart (1989), who used a 30 m 500 hPa geopotential height contour to identify closed circulation centers. Their approach used radial arms generated at 15° intervals over a great-circle distance of 2° and required that geopotential heights rise by at least 30 m along each arm. Unfortunately, the use of radial arms to define the closed contour is again sensitive to model resolution, since it has the potential to only sample as many neighbors as radial arms employed.

Here, we propose an alternative closed contour criteria that is largely insensitive to model resolution, using graph search to ensure that all paths along the unstructured grid from an initial location p0 lead to a sufficiently large decrease (or increase) in a given field G before reaching a specified radius. This criteria is illustrated in Fig. 4, and is implemented in Algorithms 4 and 5 (for closed contours around local maxima). The closed contour criteria is implemented in TempestExtremes via the command line argument --closedcontourcmd. An analogous command line argument, --noclosedcontourcmd, is also provided, which has similar functionality but discards candidates that satisfy the closed contour criteria (this may be desirable, for instance, to identify cyclonic structures that do not have a warm core).
Algorithm 4 Find the node \( p_{\text{max}} \) containing the maximal value of the field \( G \) within a distance \( \text{maxdist} \) of the node \( p \). An analogous procedure \text{find_min_near} is provided for locating nodes containing minimal values of the field.

```python
node p_{\text{max}} = \text{find_max_near}(\text{node} p, \text{field} G, \text{maxdist})
set \text{visited} = {}
set \text{tovisit} = \{p\}
p_{\text{max}} = p
while \text{tovisit} is not empty
    q = \text{remove node from tovisit}
    if (q in \text{visited}) then continue
    add q to \text{visited}
    if (\text{gcdist}(p, q) > \text{maxdist}) then continue
    if (G[q] > G[p_{\text{max}}]) then p_{\text{max}} = q
```

Algorithm 5 Determine if there is a closed contour in field \( G \) of magnitude \( \text{thresh} \) around the point \( p_0 \), defined by \( p_0 = \text{find_max_near}(p, G, \text{maxdist}) \), within distance \( \text{dist} \). That is, along all paths away from \( p_0 \), the field \( G \) must drop by at least \( \text{thresh} \) within distance \( \text{dist} \). The closed contour criteria is depicted in Fig. 4. An analogous procedure is defined for closed contours around minima.

```python
closed_contour_max(point p, field G, dist, maxdist, thresh)
p_0 = \text{find_max_near}(p, G, \text{maxdist})
set \text{visited} = {}
set \text{tovisit} = \{p_0\}
while \text{tovisit} is not empty
    q = \text{remove point from tovisit}
    if (q in \text{visited}) then continue
    add q to \text{visited}
    if (\text{gcdist}(p_0, q) > \text{dist}) then return false
    if (G[p_0] - G[q] < \text{thresh}) then
        add all neighbors of q to tovisit
    return true
```

2.7 Thresholding

Additional threshold criteria may be applied at the detection stage in order to further eliminate undesirable candidates. For example, a common threshold criteria requires that a field \( G \) satisfy some minimum value within a distance \( \text{dist} \) of the candidate, as implemented in Algorithm 6. TempestExtremes implements thresholding via the command line argument `--thresholdcmd` and includes thresholds for a particular field at candidate nodes to be greater than, less than, equal to or not equal to a specified value.

Algorithm 6 Determine if a candidate node \( p \) satisfies the requirement that there exists another node \( p_0 \) within distance \( \text{dist} \) of \( p \) with \( G[p] > \text{thresh} \).

```python
threshold_max(node p, field G, dist, thresh)
p_0 = \text{find_max_near}(p, G, dist)
if (G[p_0] < \text{thresh}) then
    return false
else
    return true
```

2.8 Stitching

The basic track stitching procedure (which represents the Reduce() stage in MapReduce) is implemented in Algorithm 7 using the output from the detection procedure at each time level (stored in set array \( \text{P}[1..T] \)). It requires additional parameters to specify a maximum great-circle distance between in-sequence nodes (\( \text{dist} \)), and a maximum gap size (\( \text{maxgap} \)). Here, gap size refers to the maximum number of sequential non-detections that can occur before a path is considered terminated. This argument is useful, for instance, for tracking tropical storms that temporarily weaken below acceptable criteria before restrengthening.

Algorithm 7 Determine all feature paths \( S \), given array of candidate nodes \( \text{P}[1..T] \) and maximum great-circle distance between nodes at subsequent time levels \( \text{dist} \).

```python
path set S = \text{stitch_nodes}(\text{set array} \text{P}[1..T], \text{dist}, \text{maxgap})
for each time level \( t = 1..T \)
    K[t] = \text{build_kd_tree}(\text{P}[t])
for each time level \( t = 1..T \)
    while \( \text{P}[t] \) is not empty
        initialize empty path \( s \)
        \( p = \text{remove next candidate from} \text{P}[t] \)
        add \( p \) into \( s \)
        gap = 0
        for time level \( u = t+1..T \)
            \( q = \text{kd_tree_nearest_neighbor}(K[u], p) \)
            if (\( q \) in \( \text{P}[u] \)) and (\( \text{gcdist}(p, q) < \text{dist} \)) then
                add \( q \) into \( s \)
                \( p = q \)
                break
            else if (\( \text{gap} < \text{maxgap} \)) then
                gap = gap + 1
            else
                break
        add \( s \) into \( S \)
```

For simplicity, \( k \)-d trees are constructed at each time level in order to maximize the efficiency of the search. Each candidate pair (time, node) can only be used in one path, and so construction simply requires exhausting the list of available
2.9 Parallelization considerations

Feature tracking fits well into a general framework known as MapReduce (Dean and Ghemawat, 2008), which is a combination of a Map(), an embarrassingly parallel candidate identification procedure applied to individual time slices, and a Reduce(), which stitches candidates across time to build feature tracks. A key advantage of employing this framework is that substantial work has been undertaken to understand optimal strategies for parallelization of MapReduce-type algorithms (e.g., Prabhat et al., 2012) in order to mitigate bottlenecks associated with I/O and load balancing. TempestExtremes currently implements a simple parallelization strategy via MPI, although future work on this issue is forthcoming. As a timing example, TempestExtremes with MPI (16 tasks) finds and tracks tropical cyclones in 10 years of 6-hourly climate data on a 0.5° latitude–longitude grid in an average of 3.8 min on the National Center for Atmospheric Research’s (NCAR’s) Yellowstone supercomputer.

3 Selected examples

Several selected examples are now provided. The first three examples use data from the NCEP Climate Forecast System Reanalysis (CFSR), available at 0.5° global resolution with 6-hourly output from 1979 to the present (Saha et al., 2010). The remaining example uses a custom variable-resolution simulation (Zarzycki and Jablonowski, 2014) (6-hourly output on a 110 km base domain that is refined to 28 km in the northern Atlantic and Pacific ocean basins) on both the native grid data and the regridded latitude–longitude grid data.
3.1 Tropical cyclones in CFSR

Our first example employs TempestExtremes for tropical cyclones (defined here as a cyclonic structure with a distinct warm core). The command line we use to detect tropical cyclone-like features in CFSR is provided below. Climate data are drawn from three files denoted $uvfile$ (containing zonal and meridional velocities), $tpfile$ (containing temperature and pressure information) and $hfile$ (containing topographic height). Three-dimensional (time plus 2-D space) hyperslabs of CFSR data have been extracted, with $\text{TMP}_L100$ corresponding to 400 hPa air temperature, and $\text{U}_\text{GRD}_L100$ and $\text{V}_\text{GRD}_L100$ corresponding to 850 hPa zonal and meridional wind velocities. Candidates are initially identified by minima in the sea level pressure ($\text{PRMSL}_L101$), and then eliminated if a more intense minimum exists within a great-circle distance of 2.0°. The closed contour criteria is then applied, requiring an increase in SLP of at least 200 Pa (2 hPa) within 4° of the candidate, and a decrease in 400 hPa air temperature of 0.4 K within 8° of the node within 1.1° of the candidate with maximum air temperature. Since CFSR is on a structured latitude–longitude grid, the output format is $i,j,\text{lon},\text{lat},\text{psl},\text{maxu},\text{zs}$, where $i,j$ are the longitude and latitude coordinates within the dataset; $\text{lon},\text{lat}$ are the actual longitude and latitude of the candidate; $\text{psl}$ is the SLP at the candidate point (equal to the maximum SLP within 0° of the candidate); $\text{maxu}$ is the vector magnitude of the maximum 850 hPa wind within 4° of the candidate; and $\text{zs}$ is the topographic height at the candidate point.

```
./DetectCyclonesUnstructured
--in_data "$uvfile;$tpfile;$hfile"
--out $outf
--searchbymin PRMSL_L101 --mergedist 2.0
--closedcontourcmd "PRMSL_L101,200.,4,0; TMP_L100,-0.4,8.0,1.1"
--outputcmd "PRMSL_L101,max,0;
_VECMAG(U_GRD_L100, V_GRD_L100),max,4;
HGT_L1,max,0"
```

All outputs from DetectCyclonesUnstructured are then concatenated into a single file containing candidates at all times (pgbhnl.dcu_tc_all.dat). Candidates are then stitched in time to form paths, with a maximum distance between candidates of 8.0° (great-circle distance), consisting of at least eight candidates per path, and with a maximum gap size of two (most consecutive time steps with no associated candidate). Because localized shallow low-pressure regions that are unrelated to tropical cyclones can form as a consequence of topographic forcing, we also require that for at least eight time steps the underlying topographic height ($\text{zs}$) be at most 100 m. The associated command line for StitchNodes is

```
./StitchNodes
--in pgbhnl.dcu_tc_all.dat
--out pgbhnl.dcu_tc_stitch.dat
--format "i,j,lon,lat,psl,maxu,\text{zs}"
```

3.2 Extratropical cyclones in CFSR

For our second example, we are interested in tracking extratropical cyclone features (defined by a cyclonic structure with no distinct warm core). The command line we have used to detect cyclonic features without the characteristic warm core of tropical cyclones (here referred to as extratropical cyclones) is given below. The command is identical to the tropical cyclone (TC) detection configuration specified in Sect. 3.1, except it requires that the feature does not possess a closed contour in the 400 hPa temperature field (no warm core).

```
./DetectCyclonesUnstructured
--in_data "$uvfile;$tpfile;$hfile"
--out $outf
--searchbymin PRMSL_L101 --mergedist 2.0
--noclosedcontourcmd "TMP_L100,-0.4,8.0,1.1"
--outputcmd "PRMSL_L101,max,0;
_VECMAG(U_GRD_L100, V_GRD_L100),max,4;
HGT_L1,max,0"
```

Stitching is similarly analogous to Sect. 3.1, except it uses a slightly more strict criteria on the underlying topographic height. The topographic filtering proved necessary in order to adequately filter out an abundance of topographically driven low pressure systems, particularly in the Himalayas region. The command line used for stitching is given below:

```
./StitchNodes
--in pgbhnl.dcu_tc_all.dat
```

Figure 5. Tropical cyclone counts within each 2° × 2° grid cell, over the period 1979–2010, obtained using the procedure described in Sect. 3.1.

```
--range 8.0 --minlength 8 --maxgap 2
--threshold "zs,\leq,100.0,8"
```

Once the complete set of tropical cyclone paths has been computed, total tropical cyclone counts over each 2° grid cell are plotted in Fig. 5. The results show very good agreement with reference fields (Gray, 1968; Knapp et al., 2010).
To 5 × wave features by requiring a drop of relative vorticity equal to 5 × 10⁻³ s⁻¹. The command line used is as follows:

```
./DetectCyclonesUnstructured
--in_data "$uvfile;$hfile" --out $outf
```

Tropical easterly waves are our third example of a pointwise feature that has been assessed in the tracking literature. In this example, Northern Hemisphere easterly waves (associated with positive relative vorticity) are tracked separately from Southern Hemisphere easterly waves (associated with negative relative vorticity). DetectCyclonesUnstructured and StitchNodes are executed separately in both hemispheres and the resultant track files concatenated. All tracking is performed on the 600 hPa relative vorticity field, using relative vorticity maxima for Northern Hemisphere waves and relative vorticity minima for Southern Hemisphere waves. Since CFSR only provides absolute vorticity, relative vorticity must first be extracted by taking the difference between absolute vorticity and the planetary vorticity (the Coriolis parameter). This is done on the command line via "_DIFF(ABS_V_L100(0),_F())", where ABS_V_L100 is the CFSR absolute vorticity variable and _F() is a built-in function for computing the Coriolis parameter (defined in _F()). In the Northern Hemisphere, we follow Thorncroft and Hodges (2001) and isolate tropical easterly wave features by requiring a drop of relative vorticity equal to 5 × 10⁻³ s⁻¹. The command line used is as follows:

```
./DetectCyclonesUnstructured
--in_pgbhnl.dcu_te_stitch.dat
--format "i,j,lon,lat,psl,maxu,zs"
--range 8.0 --minlength 8 --maxgap 2
--threshold "zs,<=.70;0,8"
```

An analogous procedure is applied in the Southern Hemisphere, except it searches for minima in the relative vorticity field and limits the latitudinal range in StitchNodes to [25S,0] for at least eight time steps. Counts of total (Northern Hemisphere plus Southern Hemisphere) tropical easterly waves within each 2° grid volume are given in Fig. 7, showing heavy wave activity throughout the Atlantic and Pacific basins. These results are very similar to other reported easterly wave densities, such as in Belanger et al. (2014) and Thorncroft and Hodges (2001), except for (a) the substantially enhanced tropical easterly wave count reported over eastern Africa (which could be eliminated by filtering over topography) and (b) essentially no observed wave activity off the western coast of South America. Nonetheless, it is well known that easterly wave climatology varies strongly across reanalysis datasets and exhibits sensitivity to the choice of tracking scheme (Hodges et al., 2003).

3.4 Tropical cyclone forecast trajectories

For our third example, we have used TempestExtremes to track forecasted tropical cyclones in numerical weather prediction simulations. Here, we show two deterministic forecasts (initialized at 00Z on 21 and 22 October 2012) for Hurricane Sandy using the Community Atmosphere Model (CAM) with a 0.125° (14 km) grid spacing over the North Atlantic basin. Details about the model setup, forecast skill of CAM, and a case study of Hurricane Sandy results can be found in Zarzycki and Jablonowski (2015). Both forecasts were initialized prior to the National Hurricane Center declaring Sandy as a tropical depression, which occurred at 12Z on 22 October (Blake et al., 2013). In Fig. 8, black dots indicate Sandy’s forecast trajectory when applying the operational tracker used by the National Centers for Environmental...
Figure 7. Tropical easterly wave counts within each $2^\circ \times 2^\circ$ grid cell, over the period 1979–2010, obtained using the procedure described in Sect. 3.3.

Figure 8. Forecast CAM trajectories for Hurricane Sandy initialized at 00Z on (a) 21 and (b) 22 October 2012. Black dots indicate trajectories defined using the NCEP operational vortex tracker with red dots denoting trajectories defined using a sample configuration of TempestExtremes.

Figure 9. An illustration of how connectivity is defined in this work for nodes on a spectral element mesh. Arrows indicate connectivity for nodes A and B.

```bash
./DetectCyclonesUnstructured
--in_data $ffile --out $outf
--mergedist 10.0
--closedcontourcmd "slp,0.5,5.0,1.0;tm,-0.1,5.0,1.0"
--outputcmd slp,min,0;_VECMAG(u850,v850),max,2;_VECMAG(u_ref,v_ref),max,2"
./StitchNodes --in cand.cyc
--out forecast.traj
--format "i,j,lon,lat,slp,wind850,windbot"
--range 6.0 --minlength 8 --maxgap 2
```

The results here demonstrate good agreement with the NCEP vortex tracker, highlighting the capability of this framework to track even pre-genesis storm features, although the sensitivity (and associated potential noise) required to find weak, shallow or sheared storms depends on the thresholds defined in DetectCyclonesUnstructured. Some differences between tracked storm centers are noted, particularly at the beginning of the forecasts, where the storm’s SLP is greater (weaker) than 1005 hPa. This is due to the fact that the pre-genesis vortex is naturally somewhat disorganized, and the NCEP tracker uses an average of multiple primary fixes (e.g., 700 and 850 hPa relative vorticity, sea level pressure, 700 and 850 hPa geopotential heights) to define the cyclone center, whereas this configuration of TempestExtremes defines storm location based on sea level pressure minimum only.

3.5 Tropical cyclones in a simulation with VR-CAM

For our final example, we assess the differences in tropical cyclone character obtained from native and regridded datasets. Using the variable-resolution spectral element option in CAM (VR-CAM-SE; Neale et al., 2012; Zarzycki et al., 2014b) to refine the Northern Hemisphere to $0.25^\circ$ resolution, a simulation of a hurricane season (June–November) has been performed. With the high-order spectral element dynamical core used to solve the fluid equations in the atmosphere, VR-CAM-SE has been demonstrated to be effective in simulating tropical cyclone-like features (Zarzycki and Jablonowski, 2014;
Figure 10. Tropical cyclone trajectories and associated intensities as obtained from the simulation of a single hurricane season in CAM 3.5 using (top) native spectral element grid data and (bottom) data regridded to a regular latitude–longitude grid with 0.25° grid spacing.

Zarzycki et al., 2014a; Zarzycki and Jablonowski, 2015). Since VR-CAM-SE uses an unstructured mesh with degrees of freedom stored at spectral element Gauss–Lobatto (GL) nodes, data are typically analyzed only after being regridded to a regular latitude–longitude mesh of approximately equal resolution. The regridding procedure has the potential to clip local extrema and smear out grid-scale features.

For this example, we use the high-order remapping package TempestRemap (Ullrich and Taylor, 2015; Ullrich et al., 2016) for remapping the native spectral element output to a regular latitude–longitude grid with 0.25° grid spacing. For purposes of determining connectivity on the variable-resolution spectral element mesh, we connect GL nodes along the coordinate axis of each quadrilateral element (see Fig. 9). DetectCyclonesUnstructured is then applied to both the native grid data and the regridded data on the regular latitude–longitude mesh (using the configuration specified in Sect. 3.1) and tropical cyclones are categorized (color-coded) by maximum surface wind speed as defined by the Saffir–Simpson scale (Simpson, 1974), such that orange and red trajectories represent the strongest classifications of storms. The results of this analysis are depicted in Fig. 10. As expected, the native grid output produces essentially identical tracks, but an increase in tropical cyclone intensity in some cases (with some tropical cyclones dropping down by a full category as a consequence of the remapping procedure and discrete nature of binning storm strength).

4 Conclusions

Automated pointwise feature trackers have been frequently and successfully employed over the past several decades to extract useful information from large climate datasets. With spatial and temporal resolution increasing rapidly in response to enhanced computational resources, climate datasets have grown increasingly unwieldy and so there has been a growing need for such large dataset processing tools. This paper has outlined a framework for pointwise feature tracking (TempestExtremes) that exposes a suite of generalized kernels drawn from the literature on trackers of the past several decades. This framework is sufficiently robust to be applicable to many climate and weather datasets, including data on unstructured grids. We expect such a framework would be useful for isolating uncertainties that emerge from particular parameter choices in tracking schemes, or to compute optimal threshold values for detecting pointwise features in, e.g., reanalysis data. Future development plans in TempestExtremes include the construction of analogous kernels for tracking areal features (blobs), such as clouds or atmospheric rivers.

5 Code availability

The open-source software described in this paper has been released as part of the TempestExtremes software package, and is available for use under the Lesser GNU Public License (LGPL). Software and examples can be obtained from GitHub at https://github.com/ClimateGlobalChange/tempestextremes.
Appendix A: A review of extratropical cyclone tracking algorithms

This appendix reviews the existing literature on extratropical cyclone tracking, one of the earliest and most common instances of both manual and automated feature tracking. Manual counts of cyclones were performed by Petterssen (1956) in the Northern Hemisphere from 1899 to 1939, and latter binned by Klein (1957) to determine the spatial distribution of such storms. These techniques were later refined by Whittaker and Horn (1982) by accounting for cyclone trajectories. A similar survey in the Southern Hemisphere was performed by Taljaard (1967) for July 1957–December 1958. Manual tracking and characterization of cyclones was also performed by Akyildiz (1985) using ECMWF forecast data for the 1981/1982 winter.

One of the first automated detection and tracking for extratropical cyclones was developed by Williamson (1981) using nonlinear optimization to fit cyclonic profiles to anomalies in the 500 mb geopotential height field. Storms were then tracked over a short forecast period using the best fit to the cyclone’s center point. Counts of cyclones neglecting the cyclone trajectory were automatically generated from climate model output for both hemispheres by Lambert (1988) using local minima in 1000 hPa geopotential height. This method had some shortcomings, including mischaracterization of local lows due to Gibbs’ ringing and topographically driven lows. To overcome these problems, Alpert et al. (1990) proposed an additional minimum threshold on the local pressure gradient. Similarly, Le Treut and Kalnay (1990) detected cyclones in ECMWF pressure data using a local minima in the sea level pressure that must also be 4 hPa below the average sea level pressure of neighboring grid points, and must persist for three successive 6 or 12 h intervals. Murray and Simmonds (1991) extracted low pressure centers from interpolated general circulation model (GCM) data using local optimization, based on earlier work in Rice (1982). These original papers primarily sought minima in the SLP field or looked for maxima in the Laplacian of the SLP field.

Several modern extratropical cyclone detection algorithms remain in use, having built on this earlier work. Short descriptions of many of these schemes are given here. Some of these algorithms use the notion of a local neighborhood or periphery, as defined in Fig. A1.

- Serreze et al. (1993); Serreze (1995) tracked cyclones in a ∼381–400 km Arctic dataset. Candidates were identified using a local minimum SLP at least 2 hPa higher than immediate neighbors. Tracking was performed with a maximum search distance of 1400 km per 12 h period.

- Sinclair (1994, 1997) tracked cyclones in a 2.5° ECMWF dataset over the Southern Hemisphere. Candidates were identified using a local minimum in the 1000 hPa geostrophic vorticity field \( \zeta_g \) (computed from the Laplacian of the 1000 hPa geopotential), adjusted for topography and the presence of heat lows (see paper for details), which further satisfied \( \zeta_g < -2 \times 10^{-5} \text{s}^{-1} \).

- Blender et al. (1997) tracked cyclones in T106 (∼125 km) ECMWF analyses. Candidates were identified using a local minimum in the 1000 hPa geopotential height field, and required to have a positive mean gradient in the 1000 hPa geopotential height field in a 1000 × 1000 km² area around each candidate. Tracking was performed using a nearest-neighbor search with a maximum displacement velocity of 80 km h⁻¹, eliminating cyclones with tracks shorter than 3 days.

- Lionello et al. (2002) tracked cyclones in a T106 (∼125 km) ECHAM-4 dataset. Candidates were identified using a local minimum in the SLP field. Tracking was performed using previous cyclone velocity to demarcate a prediction region, and candidates were discarded if they do not continue into the prediction region.

- Zolina and Gulev (2002) tracked cyclones in a T106 (∼125 km) and a T42 (∼300 km) dataset. Candidates were identified using a local minimum in the SLP field.

- Hoskins and Hodges (2002); Catto et al. (2009); Dacre et al. (2012) tracked cyclones in various reanalysis and climate datasets with wavenumber \( \leq 5 \) removed in all fields and a relative vorticity field spectrally truncated to T42. Candidates were identified from maxima in the...
850 hPa relative vorticity field. Trajectories were computed by searching for nearest neighbors and smoothed by minimizing a cost function. Cyclones were required to persist for 4 days.

- Pinto et al. (2005) tracked cyclones in T42 (~300 km) NCEP reanalysis, regridded onto a 0.75° grid by cubic spline interpolation. Candidates were identified using local minima in the pressure field that were within 1200 km of a maximum in the quasi-geostrophic relative vorticity, which was computed from the Laplacian of pressure. Candidates that were over a topography of above 1500 m were removed. They further required that the quasi-geostrophic relative vorticity was greater than 0.1 hPa/(°lat) and only the strongest candidates within 3° were retained. Cyclone tracking required a prediction velocity and search following Murray and Simmons (1991).

- Benestad and Chen (2006) tracked cyclones in 2.5° ERA40 data. Candidates were identified using multiple least-squares regression to estimate the values of the coefficients of a Fourier approximation to the SLP field (in effect a smoothing operator), followed by a 1-D search in the north–south and east–west directions.

- Simmonds et al. (2008) tracked cyclones in several 2.5° datasets over the Arctic. Candidates were identified using local minima in the Laplacian of pressure, rejecting cyclones over topography above 1000 m and requiring the presence of a nearby pressure minimum. Identified lows must satisfy a Laplacian with value > 0.2 hPa/(°lat)² over a radius of 2°. Tracking used a probability estimate using a predicted position.

Appendix B: A review of tropical cyclone tracking algorithms

More recently, and as higher-resolution climate data have become available, extratropical cyclone tracking techniques have been modified in order to support tropical cyclone tracking. To eliminate “false positives” associated with extratropical cyclones and weak cyclonic depressions, many schemes require that the candidate be associated with a nearby warm core and be associated with a minimum threshold on surface winds for at least 1–3 days. The definition of a “warm core” varies between modeling centers, including such options as air temperature anomaly on pressure surfaces (Vitart et al., 1997; Zhao et al., 2009; Murakami et al., 2012), geopotential thickness (Tsutsumi and Kasahara, 1996) and decay of vorticity with height (Bengtsson et al., 2007a; Strachan et al., 2013). Additional filtering of candidate storms over topography or within a specified latitudinal range may be required. To better match observations, additional geographical-, model- or feature-dependent criteria may be applied (Camargo and Zebiak, 2002; Walsh et al., 2007; Murakami and Sugi, 2010a; Murakami et al., 2012). It is widely acknowledged that weaker tropical storms are difficult to track, and the observational record of these less-intense, short-lived storms is questionable (Landsea et al., 2010).

A tabulated overview of the thresholds utilized by many of these schemes can be found in Walsh et al. (2007), along with several proposed guidelines on detection schemes. We extend this tabulation with the following short descriptions of many published schemes.

- Bengtsson et al. (1982) tracked tropical cyclones in one year of ~200 km forecast model output. Candidates were identified with latitude < 30° for colocated 850 hPa wind > 25 m s⁻¹ and 850 hPa relative vorticity maxima > 7 × 10⁻³ s⁻¹ in a 7.5° × 7.5° area.

- Broccoli and Manabe (1990) tracked tropical cyclones in a R15 (~600 km) dataset and a R30 (~300 km) dataset. Candidates were identified from PSL that had a 1.5 hPa local min (R15) or 0.75 hPa local min (R30), with local surface wind velocity > 17 m s⁻¹, and latitude < 30°. Tracking was performed using nearest-neighbor search with a maximum velocity of 1200 km day⁻¹.

- Wu and Lau (1992) tracked tropical cyclones in a 7.5° longitude × 4.5° latitude dataset. Candidates were identified by local minima in 1000 hPa geopotential height with a positive 950 hPa relative vorticity, negative 950 hPa divergence, positive 500 hPa vertical velocity, latitude < 40.5°, locally maximal 200 h minus 1000 hPa layer thickness that exceeded the average layer thickness within 1500 km west to east by 60 m, and 950 hPa wind greater than 17.2 m s⁻¹ locally. Tracking imposed a maximum tropical cyclone velocity of 7.5° longitude or 9° latitude per day.

- Haarsma et al. (1993) tracked tropical cyclones in a ~300 km dataset. Candidates were identified from local minimum PSL, with 850 hPa relative vorticity > 3.5 × 10⁻³ s⁻¹. Temperature anomaly ΔT was required to satisfy ΔT 250 > 0.5 K at 250 hPa, ΔT 500 > -0.5 K at 500 hPa, and ΔT 250 - ΔT 850 > -1.0 K, where the anomaly is computed against a 15° × 15° spatial mean around the center of the storm. Tracking required tropical cyclones to be persistent for a minimum of 3 days.

- Bengtsson et al. (1995, 1996) tracked tropical cyclones in a T106 (~125 km) dataset. Candidates were identified as points where 850 hPa relative vorticity > 3.5 × 10⁻³ s⁻¹, with a 850 hPa wind maximum > 15 m s⁻¹, local SLP minimum, and mean 850 hPa wind greater than mean 300 hPa wind within 7 × 7 grid points of the candidate. Temperature anomaly sum was also required to satisfy ΔT 700 + ΔT 500 + ΔT 300 > 3 K and
\[ \Delta T_{300} > \Delta T_{850} \] where the anomaly was computed against a 7 \times 7 grid-point average centered on the candidate. Tracking required tropical cyclones to be persistent for a minimum of 1.5 days.

- Tsutui and Kasahara (1996) tracked tropical cyclones in a T42 (2.8\degree, \sim 300 \text{km}) dataset. Candidates were identified as minima in the 1000 hPa geopotential height field, with at least an average drop of 20 m among neighboring points, and a further 20 m drop of average among neighboring points from periphery. Candidates were further required to satisfy that the average local 900 hPa vorticity was cyclonic, average local 900 hPa divergence was negative, average local 500 hPa vertical velocity was upward, 200 hPa minus 1000 hPa layer thickness maximum among neighbors was greater than any value in periphery, and average local 200 hPa zonal wind velocity was less than 10 m s\(^{-1}\) or local points contained at least one point with easterly velocity. The latitude of the candidate was required to be less than 40\degree, topographic height underlying candidates was less than 400 m, one local point had a 900 hPa wind speed of at least 17.2 m s\(^{-1}\), and one local point exceeded 100 mm d\(^{-1}\) over at least 1 day. Tracking required tropical cyclones to be persistent for a minimum of 2 days.

- Vitart et al. (1997, 1999, 2001, 2003) tracked tropical cyclones in a T42 (2.8\degree, \sim 300 \text{km}) dataset. Candidates were identified as 850 hPa relative vorticity maxima > 3.5 \times 10^{-5} s\(^{-1}\) with a nearby PSL minimum. They were required to possess a warm core within 2\degree latitude, defined as a local average 500 hPa to 200 hPa temperature maximum with a decrease of 0.5 K in all directions within 8\degree, and a local maximum in the 200–1000 hPa layer thickness with a decrease of 50 m in all directions within 8\degree. Tracking required the minimum distance between storms to be 800 km day\(^{-1}\), that tropical cyclones lasted at least 2 days and that the maximum wind velocity within 8\degree of the storm center must be 17 m s\(^{-1}\) for at least 2 (not necessarily consecutive) days.

- Walsh (1997); Walsh and Watterson (1997); Walsh and Katzfey (2000) tracked tropical cyclones in a 125 km regional climate dataset over Australia. Candidates were identified as points with 850 hPa relative vorticity > 2.0 \times 10^{-5} s\(^{-1}\), temperature anomaly sum \(\Delta T_{700} + \Delta T_{500} - \Delta T_{300} < 0\) K and \(\Delta T_{300} > \Delta T_{850}\), with anomaly computed against the mean over a region 2 grid points north–south and 13 grid points east–west. Candidates were also required to have 10 m surface wind > 10 m s\(^{-1}\) and 850 hPa tangential wind speed > 300 hPa tangential wind speed. Tracking required tropical cyclones to be persistent for a minimum of 2 days.

- Krishnamurti et al. (1998) tracked tropical cyclones in a T42 (\sim 300 \text{km}) climate dataset. Their approach was similar to Bengtsson et al. (1995, 1996), except using a 4 \times 4 grid-point region for the 850 hPa wind maximum, the SLP minimum and the temperature mean. Tracking required tropical cyclones to be persistent for a minimum of 1 day.

- Nguyen and Walsh (2001) assessed a 125 km regional dataset over Australia using a similar approach to Walsh and Watterson (1997). The vorticity requirement was changed to 850 hPa relative vorticity > 1.0 \times 10^{-5} s\(^{-1}\) with a PSL minimum within 250 km. Candidates also must possess a mean wind speed in a 500 km \times 500 km region at 850 hPa that was larger than mean wind speed at 300 hPa, and a mean tangential wind speed within a radius of 1\degree and 2.5\degree greater than 5 m s\(^{-1}\). Tracking required tropical cyclones to be persistent for a minimum of 1 day, with relaxed criteria after this time (see paper for further information).

- Sugi et al. (2002) tracked tropical cyclones in a T106 (\sim 125 \text{km}) climate dataset, using tracking criteria similar to Bengtsson et al. (1995). Candidates were identified by local PSL minima that was at least < 1020 hPa. Tracking required tropical cyclones to be persistent for a minimum of 2 days.

- Camargo and Zebiak (2002) tracked tropical cyclones in a T42 (\sim 300 \text{km}) climate dataset. Their approach was similar to Bengtsson et al. (1995, 1996), except with basin-specific thresholds are applied for 850 hPa relative vorticity, 850 hPa wind speed, and temperature anomaly sum \(\Delta T'_{700} + \Delta T'_{500} + \Delta T'_{300}\). Thresholds were determined by sampling the tails of probability density functions for relevant variables in each ocean basin. Following candidate identification, a relaxed 850 hPa relative vorticity threshold (> 1.5 \times 10^{-5} s\(^{-1}\)) in an area of 3 \times 3 grid points around prior detections was applied to construct trajectories. Tracking required tropical cyclones to be persistent for a minimum of 2 (1.5) days in daily (6-hourly) output.

- Tsutui (2002) tracked tropical cyclones in a T42 (2.8\degree, \sim 300 \text{km}) dataset. Their approach was similar to Tsutui and Kasahara (1996), but with simplified criteria. Candidate PSL was required to be less than the local average minus 2 hPa, and local average PSL must be less than the periphery average minus 2 hPa. Layer thickness between 200 and 700 hPa, denoted by Z, was required to satisfy \(Z_0 + \max(Z_{\pm 1\Delta}) > 2\max(Z_{\pm 2\Delta})\), where \(Z_{\pm 1\Delta}\) denotes immediate neighbors and \(Z_{\pm 2\Delta}\) denotes the periphery.

- Cheung and Elsberry (2002); Halperin et al. (2013) tracked tropical cyclones in weather forecast models using an approach similar to Walsh (1997). Candidates required a grid-point maximum in 850 hPa relative vorticity larger than all surrounding grid points within 4\degree and
either a local maximum in 200–500 hPa average temperature or 200–1000 hPa geopotential thickness that was offset by no more than 2° from the associated PSL center. In Halperin et al. (2013), tropical cyclones were required to persist for at least 24 h and have a 925 hPa horizontal wind speed greater than a model-specific threshold within 5° of the PSL center.

- Walsh et al. (2004) tracked tropical cyclones in a 30 km dataset using a similar tracking strategy to Nguyen and Walsh (2001). Candidates’ temperature anomaly was computed against a 1200 km longitude × 400 km latitude region, and the mean wind speed was computed over a 800 km × 800 km region around the storm. Candidates were further required to have local 10 m meridional velocity ≥ 17 m s⁻¹.

- McDonald et al. (2005) tracked tropical cyclones in a 2.5° latitude by 3.75° longitude dataset. Candidates were identified as local maxima in the 850 hPa relative vorticity field with magnitude greater than 5 × 10⁻⁵ s⁻¹, with temperature anomaly ΔT > 0 along the track, ΔT > 0.5 K for any two points along the track and ΔT > 0 for any two points along the track, where the anomaly was computed against a 15° × 15° mean. Tracking required that the storm’s initial latitude was < 30° and the tropical cyclones persisted for a minimum of 2 days.

- Chauvin et al. (2006) tracked tropical cyclones in a T319 (~50 km) climate time-slice simulation. Candidates were identified by local minimum PSL with 850 hPa relative vorticity > 1.4 × 10⁻⁴ s⁻¹, 850 hPa wind > 15 m s⁻¹, mean 700–300 hPa temperature anomaly ΔT > 3 K, ΔT > 0.5 K, and 850 hPa wind > 300 hPa wind. Anomalies were computed against environmental values 500 km from the cyclone center. A similar relaxation technique to Camargo and Zebiak (2002) was applied to eliminate split trajectories. Tracking required tropical cyclones to be persistent for a minimum of 1.5 days.

- Oouchi et al. (2006) tracked tropical cyclones in a 20 km dataset using a similar technique to Sugi et al. (2002). Candidate PSL was required to be 2 hPa lower than mean over 7 × 7 grid box and require a storm center of latitude < 45° with an initial position of < 30°. Near the candidate it was further required that the relative vorticity at 850 hPa was > 3.5 × 10⁻⁵ s⁻¹, the maximum wind speed at 850 hPa was > 15 m s⁻¹, the maximum wind speed at 850 hPa was larger than at 300 hPa, and the temperature anomaly sum satisfied ΔT > 2 K near the candidate. Tracking required tropical cyclones to be persistent for a minimum of 1.5 days.

- Bengtsson et al. (2007b) tracked tropical cyclones in T63, T213 and T319 datasets. Candidates were required to have 850 hPa relative vorticity minus 250 hPa relative vorticity exceed 6 × 10⁻⁵ s⁻¹, 850 hPa relative vorticity > 6 × 10⁻⁵ s⁻¹ and positive relative vorticity for all levels between 850 hPa and 250 hPa. Only Northern Hemisphere cyclones were considered (latitude < 60°). Tracking required tropical cyclones to be persistent for a minimum of 1 day.

- Knutson et al. (2007); Zhao et al. (2009) tracked tropical cyclones in a ~50 km dataset using a technique similar to Vitart et al. (1997, 2003). Candidates were required to have an absolute 850 hPa relative vorticity maxima > 1.6 × 10⁻⁴ s⁻¹ within a 6° × 6° area, a local minimum in SLP within 2° of the detection, and a maximum in average 300 hPa and 500 hPa layer temperature within 2° that was 1 K warmer than the local mean. Tracking required storms to be persistent for a minimum of 3 days, with a maximum search radius of 400 km per 6 h, and at least 3 days with a maximum surface wind speed greater than 17 m s⁻¹.

- Murakami and Sugi (2010b) tracked tropical cyclones in four datasets with resolutions from TL959 (~180 km) to TL959 (~20 km) using a procedure similar to Oouchi et al. (2006) with a resolution-dependent relative vorticity criteria.

- Caron et al. (2011, 2013) tracked tropical cyclones in a 0.3° (~35 km) climate model. Candidates were required to have a local SLP minimum (with candidates merged within 2°), 850 hPa relative vorticity > 4.0 × 10⁻⁵ s⁻¹, temperature anomalies ΔT > 0 K and ΔT > 1 K (calculated relative to 5° radial mean around the TC center), 850 hPa relative vorticity > 250 hPa relative vorticity, and a resolution-specific surface wind threshold as in Walsh et al. (2007). Tracking required storms to be persistent for a minimum of 1 day. Tracks with a relaxed set of thresholds were calculated in parallel and applied to the main tracking to minimize broken trajectories, similar to Camargo and Zebiak (2002).

- Murakami et al. (2012) tracked tropical cyclones in four datasets with resolutions from 20 to 60 km using a procedure similar to Oouchi et al. (2006) with a resolution-dependent relative vorticity and temperature anomaly criteria. Temperature anomalies were computed against a 10° × 10° grid box. Additional filtering was applied in the northern Indian Ocean by requiring maximum wind speed to be within 100–200 km of the candidate. Tracking further incorporated a maximum gap size of 1 (a single time-step failure).

- Au-Yeung and Chan (2012); Huang and Chan (2014) tracked tropical cyclones in a ~60 km dataset. Can-
candidates were identified at points with 850 hPa relative vorticity $> 4.5 \times 10^{-9}$ s$^{-1}$ and a 300 hPa temperature anomaly of 1 K defined relative to 15$^\circ$ around the vorticity center. Tracking required storms to be persistent for a minimum of 2 days and that storms originated over the ocean.

- Tory et al. (2013c, b, a) tracked tropical cyclones in several datasets at $1^\circ \times 1^\circ$ resolution. Candidates required Okubo-Weiss-Zeta parameter values $> 50 \times 10^{-6}$ s$^{-1}$ and $> 40 \times 10^{-6}$ s$^{-1}$ at 850 and 500 hPa, relative humidity $> 70\%$ and $> 50\%$ at 950 and 700 hPa, and 850–200 hPa vertical wind shear $< 25$ m s$^{-1}$. Tracking required storms to be persistent for a minimum of 2 days.

- Strachan et al. (2013) tracked tropical cyclones in several datasets from ~60 km to ~270 km. At T63 resolution, candidates were selected by 850 hPa relative vorticity $> 6 \times 10^{-5}$ s$^{-1}$, positive relative vorticity at 500 and 200 hPa, and a relative vorticity difference between 850 and 200 hPa $> 6 \times 10^{-5}$ s$^{-1}$. Tracking required storms to be persistent for a minimum of 1 day.

- Horn et al. (2014) tracked tropical cyclones in US Climate Variability and Predictability Research Program (CLIVAR) Hurricane Working Group (HWG) data (Walsh et al., 2015) (~60 km to ~110 km). Tracking was performed similar to Walsh et al. (2004), except a resolution-dependent value for surface winds was applied based on Walsh et al. (2007). Tracking required storms to originate equatorward of extratropical ridges.

- Zarzycki and Jablonowski (2014) tracked tropical cyclones in a ~28 km dataset. Candidates were selected using absolute 850 hPa relative vorticity maxima $> 1.0 \times 10^{-4}$ s$^{-1}$ with latitude $< 45$° and SLP minimum within 4°. Candidates were further required to have a local maximum 500–200 hPa average temperature within 2° of the storm center which decreases by at least 0.8 K at a radius of 5° in all directions. Tracking required storms to be persistent for a minimum of 2 days, with a maximum velocity of 400 km over 6 h, and required that the maximum surface wind speed within 4° of the candidate was greater than 17 m s$^{-1}$ for at least 2 days. Tracking also allowed a maximum gap size of 1 (a single time-step failure).

- Reed and Chavas (2015) tracked tropical cyclones on a planet in radiative-convective equilibrium. Candidates were identified using SLP minima followed by a closed contour criteria that requires a pressure increase of at least 4 hPa in all directions within 5° (great-circle distance), and using an early release of TempestExtremes.

- Bosler et al. (2016) tracked tropical cyclones in a ~14 km dataset. The tracking technique was similar to Knutson et al. (2007) and Zhao et al. (2009) except using great-circle distances for spatial calculations instead of a grid-point search.

- Harris et al. (2016) tracked tropical cyclones in multiple climate datasets with regional resolution ranging from ~75 km to ~10 km. Candidates were identified from a minimum smoothed SLP no greater than 1013 hPa with 2 hPa closed contour not encircling another minimum. Candidates were further required to have 2 K closed contour around 300–500 hPa temperature maximum within 500 km and an 850 hPa relative vorticity $> 1.5 \times 10^{-4}$ s$^{-1}$. Cyclones were tracked for a minimum of 3 days, with a maximum search radius of 750 km per 6 h, and required at least 1.5 consecutive days with a maximum surface wind speed greater than 17.5 m s$^{-1}$, following Chen and Lin (2011).

Appendix C: A (short) review of tropical easterly wave tracking algorithms

Tropical easterly waves are featured more sparsely within the literature, but are nonetheless an important pointwise feature in climate datasets. Pointwise tracking is complementary to statistical techniques which typically examine the variability, for instance, in the African easterly jet (AEJ) (i.e., Ceron and Gueremy, 1999). The first manual study that identified and tracked African easterly wave was performed by Reed et al. (1988) using positive relative vorticity anomalies. This strategy was also applied by Thornicroft and Hodges (2001), Hodges et al. (2003) and Serra et al. (2010). Other studies have used curvature vorticity anomalies (Agudelo et al., 2011; Belanger et al., 2014; Bain et al., 2014; Brammer and Thornicroft, 2015) and stream functions (Berry et al., 2007).

Appendix D: Software documentation: DetectCyclonesUnstructured

This section contains the software documentation for the executable DetectCyclonesUnstructured from the TempestExtremes package. The software is provided for use within a command-line shell, such as bash.

Usage: DetectCyclonesUnstructured <parameter list>

Parameters: --in_data <string> [""]
--in_data_list <string> [""]
--in_connect <string> [""]
--out <string> [""]
--out_file_list <string> [""]
--searchbymin <string> [""] (default PSL)
--searchbymax <string> [""]
--minlon <double> [0.000000] (degrees)
--maxlon <double> [0.000000] (degrees)
--minlat <double> [0.000000] (degrees)
--maxlat <double> [0.000000] (degrees)
--minabslat <double> [0.000000] (degrees)
--topofile <string> [""]
--maxtopoht <double> [0.000000] (m)
--mergedist <double> [0.000000] (degrees)
--closedcontourcmd <string> ["]"
  [var,delta,dist,minmaxdist;...]  
--noclosedcontourcmd <string> ["]"
  [var,delta,dist,minmaxdist;...]  
--thresholdcmd <string> [""
  [var,op,value,dist;...]  
--outputcmd <string> [""
  [var,op,dist;...]  
--timestride <integer> [1]
--regional <bool> [false]
--out_header <bool> [false]
--verbosity <integer> [0]

--in_data <string> is a list of input data files in NetCDF format, separated by semicolons.

--in_data_list <string> is a file containing the --in_data argument for a sequence of processing operations (one per line).

--in_connect <string> is a connectivity file, which uses a vertex list to describe the graph structure of the input grid. This parameter is not required if the data are on a latitude–longitude grid.

--out <string> is the output file containing the filtered list of candidates in plain text format.

--out_file_list <string> is a file containing the --out argument for a sequence of processing operations (one per line).

--searchbymin <string> is the input variable to use for initially selecting candidate points (defined as local minima). By default, this is “PSL”, representing detection of surface pressure minima. Only one of searchbymin and searchbymax may be set.

--searchbymax <string> is the input variable to use for initially selecting candidate points (defined as local maxima). Only one of searchbymin and searchbymax may be set.

--minlon <double> is the minimum longitude for candidate points.

--maxlon <double> is the maximum longitude for candidate points.

--minlat <double> is the minimum latitude for candidate points.

--maxlat <double> is the maximum latitude for candidate points.

--minabslat <double> is the minimum absolute latitude for candidate points.

--mergedist <double> merges candidate points with distance (in degrees) shorter than the specified value. Among two candidates within the merge distance, only the candidate with lowest searchbymin or highest searchbymax value will be retained.

--closedcontourcmd <cmd1>;<cmd2>;... Eliminate candidates if they do not have a closed contour. Closed contour commands are separated by a semicolon. Each closed contour command takes the form var,delta,dist,minmaxdist. These arguments are as follows.

  var <variable> is the variable used for the contour search.

  dist <double> is the great-circle distance (in degrees) from the pivot within which the closed contour criteria must be satisfied.

  delta <double> is the amount by which the field must change from the pivot value. If positive (negative) the field must increase (decrease) by this value along the contour.

  minmaxdist <double> is the distance away from the candidate to search for the minima/maxima. If delta is positive (negative), the pivot is a local minimum (maximum).

--noclosedcontourcmd <cmd1>;<cmd2>;... is the same as closedcontourcmd, except it eliminates candidates if a closed contour is present.

--thresholdcmd <cmd1>;<cmd2>;... eliminates candidates that do not satisfy a threshold criteria (there must exist a point within a given distance of the candidate that satisfies a given equality or inequality). Threshold commands are separated by a semicolon. Each threshold command takes the form var,op,value,dist. These arguments are as follows.

  var <variable> is the variable used for the contour search.

  op <string> is an operator that must be satisfied for threshold (options include >, >=, <, <=, =, !=).

  value <double> is the value on the right-hand side (RHS) of the comparison.

  dist <double> is the great-circle distance away from the candidate to search for a point that satisfies the threshold (in degrees).

--outputcmd <cmd1>;<cmd2>;... includes additional columns in the output file. Output commands take the form var,op,dist. These arguments are as follows.
var <variable> is the variable used for the contour search.

op <string> is an operator that is applied over all points within the specified distance of the candidate (options include max, min, avg, maxdist, mindist).

dist <double> is the great-circle distance away from the candidate wherein the operator is applied (in degrees).

--timestride <integer> only examines discrete times at the given stride (by default 1).

--regional is used when a latitude–longitude grid is employed, to not assume longitudinal boundaries to be periodic.

--out_header outputs a header describing the columns of the data file.

--verbosity <integer> sets the verbosity level (default 0).

D1 Variable specification

Quantities of type <variable> include both NetCDF variables in the input file (for example, “Z850”) and simple operations performed on those variables. By default, it is assumed that NetCDF variables are specified in the .nc file as float Z850(time, lat, lon) or float Z850(time, ncol) for structured latitude–longitude grids and unstructured grids, respectively. If variables have no time variable, they have the related specification float Z850(lat, lon) or float Z850(ncol). If variables include an additional dimension, for instance, float Z(time, lev, lat, lon) or float Z(time, lev, ncol) they may be specified on the command line as Z<lev>, where the integer index <lev> corresponds to the first dimension (or the dimension after time, if present).

Simple operators are also supported, including

_ABS(<variable>) absolute value of a variable,

_AVG(<variable>, <variable>) pointwise average of variables,

_DIFF(<variable>, <variable>) pointwise difference of variables,

_F() Coriolis parameter,

_MEAN(<variable>, <distance>) spatial mean over a given radius,

_PLUS(<variable>, <variable>) pointwise sum of variables, and

_VECMAG(<variable>, <variable>) two-component vector magnitude.

For instance, the following are valid examples of <variable> type,

_MEAN(PSL, 2.0),
_VECMAG(U850, V850)
and
_DIFF(U(3), U(5)).

D2 MPI support

The DetectCyclonesUnstructured executable supports parallelization via MPI when the --in_data_list argument is specified. When enabled, the parallelization procedure simply distributes the processing operations evenly among available MPI threads.

Appendix E: Software documentation: StitchNodes

This section contains the software documentation for the executable StitchNodes from the TempestExtremes package.

Usage: StitchNodes <parameter list>

Parameters:

--in <string> [""]
--out <string> [""]
--format <string> ["no,i,j,lon,lat"]
--range <double> [5.000000] (degrees)
--minlength <integer> [3]
--min_endpoint_dist <double> [0.000000] (degrees)
--min_path_dist <double> [0.000000] (degrees)
--maxgap <integer> [0]
--threshold <string> ["""] [col,op,value,count;...]
--timestride <integer> [1]
--out_format <string> ["std"] (std|visit)

--in <string> is the input file (a list of candidates from DetectCyclonesUnstructured).

--out <string> is the output file containing the filtered list of candidates in plain text format.

--format <string> is the structure of the columns of the input file.

--range <double> is the maximum distance between candidates along a path.

--minlength <integer> is the minimum length of a path (in terms of number of discrete times).

--min_endpoint_dist <double> is the minimum great-circle distance between the first candidate on a path and the last candidate (in degrees).
--min_path_dist <double> is the minimum path length, defined as the sum of all great-circle
distances between candidate nodes (in degrees).

--maxgap <integer> is the largest gap (missing candidate nodes) along the path (in discrete time
points).

--threshold <cmd1>;<cmd2>;... eliminates paths that do not satisfy a threshold crite-
rion (a specified number of candidates along path must satisfy an equality or inequality). Threshold commands
are separated by a semicolon. Each threshold command
takes the form col,op,value,count. These arguments are as follows.

  col <integer> is the column in the input file
to use in the threshold criteria.
  op <string> is an operator used for comparison
  of column value (options include >, >=, <, <=, =, !=).
  value <double> is the value on the right-hand
  side of the operator.
  count <integer> is the minimum number of
  candidates along the path that must satisfy this cri-
teria.

--timestride <integer>
only examines discrete times at the given stride (by de-
default 1).
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1088 P. A. Ullrich and C. M. Zarzycki: A framework for scale-insensitive pointwise feature tracking


