Radiation sensitivity tests of the HARMONIE 37h1 NWP model

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Received: 25 October 2013 – Published in Geosci. Model Dev. Discuss.: 17 December 2013
Revised: 21 May 2014 – Accepted: 2 June 2014 – Published: 16 July 2014

Abstract. When short-wave (SW) radiation fluxes modelled with a numerical weather prediction (NWP) model or climate model do not match observed SW fluxes it can be challenging to find the cause of the differences. Several elements in the model affect SW fluxes. This necessitates individual testing of each of the physical processes in the NWP model. Here we present a focused study of the SW radiation schemes in the HIRLAM (HIgh Resolution Limited Area Model) Aladin Regional Mesoscale Operational NWP In Europe (HARMONIE) model, which is the primary NWP model used and developed by several National Weather Services in Europe. Detailed calculations have been made with the DISORT model run in the libRadtran framework, which is a collection of state-of-the-art radiative transfer software and data sets. These are used to test the NWP radiation calculations. Both models are given the same atmospheric properties as input. We also perform a separate test of cloud liquid optical property parameterisations with Mie calculations. This leads us to introduce a new parameterisation for calculating these properties. In addition, we show that the results of a simpler radiation scheme, introduced into HARMONIE, compare well with those of the comprehensive default parameterisations. The methodology applied here may be used for testing radiation schemes in other NWP or climate models.

1 Introduction

One of the main problems in comparing numerical weather prediction (NWP) models to observations is that there is generally a long chain of elements in the models that leads to the given results. This is also true for modelled solar radiation fluxes. Biases in the predicted downwelling, reflected and net short-wave (SW) fluxes could be due to atmospheric radiative transfer calculations. However, errors could also be related to incorrect input to the radiation calculations: incorrect cloudiness (liquid or ice water loads and their distributions) or poorly known properties of the clouds (size and shape of the cloud particles), which influence the SW transmittance and absorptance. Under clear sky conditions, atmospheric aerosol loads and aerosol optical properties may not be described completely. Surface radiative properties like albedo may be represented inaccurately, for example because of poor knowledge of the existence of snow and ice cover on land and water surfaces. The amount of soil moisture or the treatment of evaporation could affect the formation and lifetime of clouds and fog, which indirectly affect the radiation fluxes. Very often multiple solutions exist for correcting an observed SW bias, where several of the mentioned parameterisations or assumptions can be tuned to correct a given bias. This equifinality needs to be resolved. One way of doing this is by testing each of physical processes in the NWP model separately. Here we present a focused study of one component of the HIRLAM (HIgh Resolution Limited Area Model) Aladin Regional Mesoscale Operational NWP In Europe (HARMONIE) modelling system, i.e. the SW radiation scheme. Our particular focus on this component is because it has not previously been studied in the HARMONIE modelling system.

Correctly modelling the SW radiative transfer in an NWP model depends firstly on correctly describing the state of the atmosphere and the surface. In particular cloud liquid water and cloud ice concentrations (L’Ecuyer et al.,
2008) are important, but cloud effective radius (Hansen and Travis, 1974; Hu and Stamnes, 1993), cloud ice effective size (Fu, 1996), cloud ice particle shape and size distributions (Kahnhert et al., 2008), water vapour (Pierluissi and Peng, 1985), aerosols (Shettle, 1989; Hess et al., 1998; Reddy et al., 2005; Myhre et al., 2007), ozone (Forster et al., 2007), surface reflectance (Sagan and Pollack, 1967; Thomas and Stamnes, 2002), Sun–Earth distance, air pressure, altitude and position of the Sun relative to the given topography (Senkova et al., 2007; Manners et al., 2012) can also significantly affect the net and downward global radiation. Secondly, when the atmospheric state is known, the optical properties of particles and gases in the atmosphere need to be correctly calculated. Thirdly, a sufficiently accurate radiative transfer scheme is needed to estimate the solar radiation fluxes.

Here we focus on the second and third steps described above, by testing various radiation parameterisations, available in the HARMONIE NWP model, against the accurate one-dimensional radiative transfer model, DISORT (Stamnes et al., 1988, 2000) in prescribed atmospheric conditions. Since not all of the radiation schemes available in HARMONIE perform the second and third steps separately, we primarily present tests of these two steps together. DISORT is run within the framework of the libRadtran library (Mayer and Kylling, 2005)\(^1\). It solves the radiative transfer (the third step), while various parameterisations in libRadtran are used to calculate the optical properties (the second step). In addition to using libRadtran/DISORT we also perform separate Mie calculations with the solver of Wiscombe (1980) in order to perform direct tests of the liquid cloud optical property calculations in HARMONIE.

The HARMONIE NWP system combines elements from the global IFS/Arpege model (Déqué et al., 1994) with the ALADIN nonhydrostatic dynamics (Bénard et al., 2010) and physical parameterisations of AROME (Seity et al., 2011) and HIRLAM (Undén et al., 2002). Here IFS is an abbreviation of Integrated Forecast System, ALADIN is an abbreviation of Aire Limitée Adaptation dynamique Développement InterNational and AROME is an abbreviation of Applications of Research to Operations at Meoscale. In the current version (37h1), the default SW radiation scheme is based on the radiation transfer code in the Integrated Forecast System (IFS cycle 25R1, European Centre for Medium-Range Weather Forecast implementation in 2002), see ECMWF (2012) and Mascart and Bougeault (2011). This is a comprehensive, but also computationally demanding, scheme with several spectral bands both in the solar and terrestrial radiation ranges. In the following, we refer to this as the IFS radiation scheme. Here we test this scheme and also the alternative HIRLAM radiation scheme, further denoted as hlradia, which is based on Savijärvi (1990). Hlradia is a simple and computationally fast radiation parameterisation, where the cloud transmittance and absorptance are calculated using the parameterisation of Wyser et al. (1999).

Oreopoulos et al. (2012) recently compared a large set of SW and long-wave radiation schemes that are currently used in atmospheric models. In their tests, realistic atmospheric profiles from the Atmospheric Radiation Measurement programme were used. Here we use idealised cases which are not necessarily realistic. The advantage of using idealised cases is that the full range of sensitivity can be tested for each of the relevant variables individually. Fixed atmospheric states and surface properties are used both in HARMONIE and in DISORT.

In practice, a simple radiation scheme applied at each time step (currently 1 min) of the model integration requires as much computation time as a complicated scheme called a few times an hour. The accuracy requirements for radiation parameterisations in long-term climate simulations on relatively coarse spatial and temporal scales differ from those of the kilometre-scale short-term NWP models run in continuous data assimilation forecast cycles. For example, the importance of quickly changing cloud–radiation interactions may be greater in the latter while the former requires maximum accuracy in handling the details of gaseous transmission. It is thus of interest to understand and compare the accuracy of the simple and complex schemes against a good reference. Such a reference for testing the HARMONIE SW radiation parameterisations was obtained by applying the libRadtran/DISORT model. The computations done by the detailed radiative transfer model also provide valuable information about the sensitivity of SW radiation fluxes to a wide range of various atmospheric properties.

2 Methods

Different SW radiation schemes currently available in the HARMONIE framework were compared with libRadtran/DISORT results for 11 experiments. The experiments can be split into three groups: clear sky experiment 1–3, liquid cloud experiment 4–7, and ice cloud experiment 8–11. In each of the experiments the sensitivity to a different variable was studied as outlined in Table 1.

2.1 DISORT

The DISORT algorithm was run for the full SW spectrum using the Kato et al. (1999) correlated-k algorithm, which includes absorption coefficients from the HITRAN 2000 database and an angular discretisation of 30 streams. For experiment 2 we used the pseudo-spherical version of DISORT (Dahlback and Stamnes, 1991) in order to account for the sphericity of Earth’s atmosphere at higher solar zenith angles.

We used the Hu and Stamnes (1993) parameterisation that is accurate to within 1 % with respect to full spectrum SW
fluxes to calculate the liquid cloud optical properties. We used the Fu (1996) parameterisation to calculate the ice optical properties for DISORT.

In the following we will refer to the libRadtran/DISORT clear sky results as Kato-DISORT, the liquid cloud results as HS-DISORT, and the ice cloud results as Fu-DISORT, in order to emphasise the primary parameterisations used in libRadtran to calculate the optical properties for DISORT.

2.2 Default IFS radiation scheme in HARMONIE

The default IFS radiation scheme in HARMONIE has six SW spectral bands: three bands in the ultraviolet and visible spectral ranges and three bands in the solar infrared spectral range. Specifically, these six spectral bands are defined by the wavelengths 0.185–0.25–0.44–0.69–1.19–2.38–4.00 µm (Mascart and Bougeault, 2011). At the top of the atmosphere each of these bands have 0.19, 13.57, 32.21, 32.62, 18.06 and 5.40 of the SW flux, respectively. The top of atmosphere SW flux is calculated using the formulae of Fouquart and Bonnel (1980) for each of the six SW spectral bands parameterisation. Alternatively, the Mie scattering parameterisation by Joseph et al. (1976) and in Table 1. The benchmark radiative transfer experiments.

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Variable</th>
<th>Range</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>Integrated water vapour</td>
<td>0.32–32 kg m⁻²</td>
</tr>
<tr>
<td>2</td>
<td>Solar zenith angle</td>
<td>0–80°</td>
</tr>
<tr>
<td>3</td>
<td>Surface albedo (clear sky)</td>
<td>0.0–0.8</td>
</tr>
<tr>
<td>4</td>
<td>Cloud liquid water</td>
<td>0–5 kg m⁻²</td>
</tr>
<tr>
<td>5</td>
<td>Cloud drop eff. radius</td>
<td>4–40 µm</td>
</tr>
<tr>
<td>6</td>
<td>Surface albedo (cloudy sky: (cloud water load 0.1 kg m⁻²)</td>
<td>0.0–0.8</td>
</tr>
<tr>
<td>7</td>
<td>Surface albedo (thick cloud: (cloud water load 1.0 kg m⁻²)</td>
<td>0.0–0.8</td>
</tr>
<tr>
<td>8</td>
<td>Cloud ice (albedo=0.18)</td>
<td>0–0.5 kg m⁻²</td>
</tr>
<tr>
<td>9</td>
<td>Cloud ice (albedo=0.7)</td>
<td>0–0.5 kg m⁻²</td>
</tr>
<tr>
<td>10</td>
<td>rₑ,ice (albedo=0.18)</td>
<td>20–80 µm</td>
</tr>
<tr>
<td>11</td>
<td>rₑ,ice (albedo=0.7)</td>
<td>20–80 µm</td>
</tr>
</tbody>
</table>

Supplement Part 1. In the IFS radiative transfer calculations the key input variable is the scaled optical depth τ∗ᵢ, which is a product of the optical depth τᵢ and the delta-Eddington scaling factor (1 − ωᵢ gᵢ²) (Joseph et al., 1976):

\[ τᵢ = (1 − ωᵢ gᵢ²) τᵢ \]

\[ τᵢ = βᵢ C, \]

where, according to the suggested new scheme,

\[ βᵢ = aᵢ rₑ,liq⁻bᵢ \]

\[ ωᵢ = cᵢ - dᵢ rₑ,liq \]

\[ gᵢ = eᵢ + fᵢ rₑ,liq - hᵢ \exp (- jᵢ rₑ,liq). \]

Here, i denotes the wavelength band index, ωᵢ is the single scattering albedo, gᵢ is the asymmetry factor, βᵢ is the mass extinction coefficient in m² g⁻¹ and C is the mass load in g m⁻², rₑ,liq is the cloud droplet effective radius, and aᵢ, bᵢ, cᵢ, dᵢ, eᵢ, fᵢ, hᵢ and jᵢ are coefficients as detailed in Table 2.

As can be seen in Eq. (2), the asymmetry factor gᵢ is important for the scaling factor. For this reason we have made a more comprehensive empirical formula for gᵢ in Eq. (5) than those used in the Fouquart (1987) and Slingo (1989) parameterisations, where gᵢ is given as constants in the former and as linear functions of rₑ in the latter.

The parameterisation for wavelength band 1 (0.185–0.25 µm) is irrelevant, as virtually no SW irradiance at these wavelengths reaches the levels of the lower atmosphere, where clouds occur. This is why it is omitted in Table 2.

2.3 HIRLAM radiation scheme (hlradia)

A slightly modified version of the HIRLAM radiation scheme hlradia as compared to the original version (Undén et al., 2002) was used in our tests in the HARMONIE framework. In hlradia one SW spectral band is considered and both the clear sky and cloudy sky transmittances and absorptances are parameterised in order to make the scheme very fast (Savijärvi, 1990; Wyser et al., 1999). The impact of ozone, oxygen and carbon dioxide, as well as aerosols, on SW irradiance is assumed to be constant over time and


Table 2. Coefficients used for the Nielsen liquid cloud optical parameterisation. The columns show the wavelength bands (i) 2–6.

<table>
<thead>
<tr>
<th>i</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
</tr>
</thead>
<tbody>
<tr>
<td>µm</td>
<td>0.25–</td>
<td>0.44–</td>
<td>0.69–</td>
<td>1.19–</td>
<td>2.38–</td>
</tr>
<tr>
<td>aᵢ</td>
<td>1.606</td>
<td>1.638</td>
<td>1.685</td>
<td>1.77</td>
<td>1.87</td>
</tr>
<tr>
<td>bᵢ</td>
<td>1.015</td>
<td>1.019</td>
<td>1.024</td>
<td>1.035</td>
<td>1.046</td>
</tr>
<tr>
<td>cᵢ</td>
<td>1.000</td>
<td>1.000</td>
<td>0.99999</td>
<td>0.9985</td>
<td>0.823</td>
</tr>
<tr>
<td>dᵢ</td>
<td>3.3 × 10⁻¹</td>
<td>10 × 10⁻⁴</td>
<td>1.49 × 10⁻⁵</td>
<td>9.2 × 10⁻⁴</td>
<td>0.004</td>
</tr>
<tr>
<td>eᵢ</td>
<td>0.868</td>
<td>0.868</td>
<td>0.867</td>
<td>0.864</td>
<td>0.886</td>
</tr>
<tr>
<td>fᵢ</td>
<td>1.4 × 10⁻¹</td>
<td>2.5 × 10⁻⁴</td>
<td>3.1 × 10⁻⁴</td>
<td>5.4 × 10⁻⁴</td>
<td>0.0011</td>
</tr>
<tr>
<td>hᵢ</td>
<td>0.061</td>
<td>0.063</td>
<td>0.078</td>
<td>0.133</td>
<td>0.20</td>
</tr>
<tr>
<td>jᵢ</td>
<td>0.25</td>
<td>0.25</td>
<td>0.195</td>
<td>0.194</td>
<td>0.18</td>
</tr>
</tbody>
</table>
space. Cloud transmittance and absorptance are calculated based on empirically derived functions of cloud condensate content and cloud particle effective radii. They are integrated vertically from the top of the atmosphere to each level, combining cloud liquid and ice particles. Thus within hlradia, the calculation of cloud optical properties and the radiative transfer calculation are not separable.

3 Experiments and initial atmospheric conditions

MUSC, the single column version of HARMONIE, based on Malardel et al. (2006), was used as a framework to provide the radiation schemes with the atmospheric and surface input data. A vertical resolution of 41 full model levels (in pressure-based hybrid coordinates) between the surface and an elevation of 100 km was used (Undén, 2010). Hybrid coordinates follow the topography at the lowest levels and converge towards isobaric levels higher in the atmosphere (Holton, 1992). The same model levels were used in the DISORT calculations. Only output from the first time step of MUSC was used in order to exclude the influence of an evolving atmospheric state on the results.

The reference (initial) definitions for the HARMONIE and libRadtran/DISORT experiments are:

- Day of year = 79, i.e. the 20 March or vernal equinox
- Altitude = 0.0 km above sea level
- Solar zenith angle = 56°
- Surface albedo = 0.18
- Clear sky
- “Mid-latitude summer” atmospheric profile from Anderson et al. (1986), including geopotential heights, temperature, air densities, mixing ratios of water vapour, ozone, oxygen and carbon dioxide from the surface to the top of the atmosphere assumed to be at 120 km.

Water vapour input data were interpolated to the model levels, keeping the vertical distribution unchanged when modifying the vertically integrated load in the experiments. In experiment 1 (integrated water vapour) we also tested the effect of using the “mid-latitude winter” atmospheric profile (Anderson et al., 1986).

In order to make the sensitivity experiments as simple as possible, all clouds were assumed to be homogeneous, to be situated between 1 and 2 km above the surface, and to have prescribed properties. The prescribed properties comprise vertically integrated specific cloud liquid and ice content, a constant liquid droplet effective radius and a constant ice crystal equivalent radius (Table 1). Such clouds may be unrealistic and in contradiction to the assumed water vapour distribution. However, our aim here is not to test realistic experiments, but rather to make focused tests of the radiation schemes in HARMONIE. Using idealised clouds also enables us to test a wider variety of cloud types than if we, for instance, had used cloud data from measurement campaigns.

Aerosols are described differently in each of the three radiation schemes: in libRadtran/DISORT the Shettle (1989) rural aerosol profile is used, in the HARMONIE IFS scheme an aerosol climatology (Tanré et al., 1984; Mascart and Bougeault, 2011) is applied and in hlradia aerosols are represented by constant coefficients (Savijärvi, 1990). As these cannot be compared in detail, i.e. for various aerosol types and concentrations, we have excluded aerosols from this study.

4 Results and discussion

In the following sections the total downward SW irradiance at the surface on a horizontal plane, i.e. the global radiation [W m$^{-2}$], is presented for each of the 11 radiation sensitivity experiments (Table 1). In addition, net fluxes on model levels are presented for a select number of the experiments. Net fluxes, defined as the downward SW fluxes minus the upward SW fluxes, are presented as % differences relative to the libRadtran/DISORT results. The clear sky experiments are discussed in Sect. 4.1 and cloud liquid and cloud ice experiments are discussed in Sects. 4.2 and 4.3, respectively. In these experiments when the cloud condensate is > 0 kg m$^{-2}$ the fractional cloud cover was set to 1. In Sect. 4.4 the results of tests of the IFS delta-Eddington scheme against DISORT are shown and discussed.

4.1 Clear sky experiments

Three clear sky experiments were carried out to test the SW radiation sensitivity to water vapour (experiment 1), solar zenith angle (experiment 2) and surface albedo (experiment 3).

4.1.1 Experiment 1: water vapour

In the water vapour experiment (experiment 1), the agreement between the IFS radiation scheme and Kato-DISORT is very good for the highest water vapour loads but has a negative bias of 2 % or 15 W m$^{-2}$ at the lowest water vapour load. Hlradia has a positive bias of 3.5 % or 20 W m$^{-2}$ relative to Kato-DISORT at the highest water vapour load, but lower bias at the lower water vapour loads (Fig. 1). When the “mid-latitude summer” atmospheric profile is replaced with the “mid-latitude winter” atmospheric profile a decrease of approximately 0.5 % or less in global radiation is seen in all three models in Fig. 1. The primary reason for this decrease is pressure broadening of the water vapour absorption lines (Thomas and Stamnes, 2002). The absorption is saturated quickly near the line centres; pressure broadened
absorption lines cover the vast spectral regions between lines better (Chou and Kouvaris, 1986). This shows that the vertical distribution of the water vapour in the atmosphere is also important for the clear sky transmittance. Since the “mid-latitude winter” atmosphere cannot contain the highest water vapour loads there are fewer points for this in Fig. 1. The height level net flux deviation of IFS from Kato-DISORT (Fig. 2) varies from approximately 0.0 % at the top of the atmosphere to the negative biases also seen in Fig. 1 for the lowest water vapour loads at the surface. The hlradia net flux differences are between 0.0 and +3.0 % (Fig. 3). In all of the following experiments the “mid-latitude summer” profile was used.

Gases other than water vapour affect the SW radiation. The most important of these is ozone. We have tested the SW sensitivity to ozone by running Kato-DISORT. Here the ozone cross-section parameterisation of Bass and Paur (1985) was used. When ozone was reduced from 500 Dobson units (DU) to 100 DU, the global radiation at the surface increased by 2.3 %. Since 500 and 100 DU are extreme values of the ozone layer thickness, we find that there is little error in using climatological ozone data (as is done in the IFS radiation scheme), or in using constant ozone SW absorption (as is done in hlradia). In an hlradia experiment, a complete removal of the ozone absorption led to an increase in the global radiation at the surface of 4.5 %. Detailed UVB/UV A estimations are not needed in general NWP computations, since only the net fluxes at the model levels influence the simulated temperatures.

The variations in carbon dioxide and oxygen are practically irrelevant for SW radiation in NWP modelling, because they only affect the extreme fringes of the IR and UV parts of the solar spectrum, respectively. As an example we tested the sensitivity of SW radiation to carbon dioxide concentration with Kato-DISORT. The carbon dioxide concentration is set to 330 ppm in the “mid-latitude summer” profile from Anderson et al. (1986). In both IFS and hlradia, this is set to be 353 ppm. Increasing the carbon dioxide concentration in Kato-DISORT from 330 to 353 ppm causes a relative...
Figure 4. As for Fig. 1 but for the solar zenith angle (experiment 2). The vertical dashed line marks the reference solar zenith angle used in the other experiments. The subplot shows the corresponding relative differences defined as $(X - \text{DISORT}) / \text{DISORT} \cdot 100\%$.

Figure 5. As for Fig. 1 but for surface albedo (experiment 3). The vertical dashed line at 0.18 marks the reference albedo used in experiment 1–3, 5–6, 9 and 11. The vertical dashed line at 0.7 marks the albedo used in experiment 10 and 12.

Figure 6. As for Fig. 2 but for IFS compared to Kato-DISORT as a function of surface albedo (experiment 3).

decrease of 0.01 % in the surface downward global SW radiation. The relative impact of changing the oxygen concentration on the surface downward global SW radiation is even less. In an hlradia experiment, the effect of doubling the CO$_2$ concentration on the SW radiation fluxes was negligible.

4.1.2 Experiment 2: solar zenith angle

The solar zenith angle (SZA) experiment (experiment 2, Fig. 4) shows agreement between the IFS global radiation and Kato-DISORT of better than 1.0 % for most of the SZAs. Hlradia shows a systematic overestimation of +2 to +5 %.

4.1.3 Experiment 3: surface albedo – clear sky case

In experiment 3 the sensitivity of varying the surface albedo in clear sky conditions was tested (Fig. 5). The relative difference for the IFS radiation scheme compared to Kato-DISORT is less than 1 % for all surface albedos. For the hlradia radiation scheme the relative differences range from +3 to +4.5 %, increasing with increasing albedo. The differences in net fluxes as a function of height in the atmosphere are shown in Figs. 6 and 7 for the IFS and the hlradia radiation schemes, respectively, relative to Kato-DISORT. These differences are mostly less than 2 % for the IFS radiation scheme and less than +5 % for the hlradia scheme but they decrease for the higher surface albedos.

4.2 Liquid cloud experiments

Four liquid cloud experiments were run to test the SW radiation sensitivity to cloud water load, cloud drop effective radius ($r_{e,\text{liq}}$) and surface albedo. Tests of the surface albedo sensitivity were run for both the case of a cloud of medium thickness (cloud water load 0.1 kg m$^{-2}$) and the case of a thick cloud (cloud water load 1.0 kg m$^{-2}$).

4.2.1 Mie experiments

In Fig. 8 the results of tests of the HARMONIE IFS cloud liquid optical property parameterisations for spectral band 4 (690–1190 nm) are shown. It can be seen that there are significant differences between the parameterisations, and that a better fit to the Mie calculations can be obtained with our “Nielsen” parameterisation (Eqs. 3–5 and Table 2). The details of these Mie calculations and the results for the other spectral bands can be found in the Supplement Part 1.
4.2.2 Experiment 4: cloud water load

Experiment 4 was run to test the cloud water load sensitivity. A fixed $r_{e,liq}$ of 10 µm was used, which is a typical value for stratocumulus clouds (e.g. Martin et al., 1994). Before being used for SW radiation calculations the cloud water load is multiplied by a so-called cloud SW inhomogeneity factor of 0.7 in the default SW scheme of HARMONIE 37h1. In hlradia, a SW inhomogeneity factor of 0.8 is used by default. After several tests, it became clear that the SW inhomogeneity factor is very significant. We therefore performed an additional test showing the effect of changing the inhomogeneity factor (Fig. 9 and Table 3).

For cloud water loads of 0.05 to 0.1 kg m$^{-2}$ the transmitted global radiation is almost 50 W m$^{-2}$ higher with the SW inhomogeneity factor set to 0.7, compared to when it is set to 1.0, for the case where the default Harmonie radiation settings are used, i.e. IFS with the Fouquart cloud optical property parameterisation (Fouquart, 1987). Similarly, when the hlradia scheme is used with a SW inhomogeneity factor of 1.0 rather than 0.8, the global radiation is more than 30 W m$^{-2}$ less. Note that in our experiments, where cloud water load is given as an input value, application of an inhomogeneity factor means reduction of this predefined input by 20 % (hlradia) or 30 % (IFS).

Overall, when the cloud SW inhomogeneity factor is set to 1.0, the results are closer to those from HS-DISORT. This is not surprising, as the HS-DISORT tests were done for horizontally homogeneous clouds. In both the Meso-NH model (Mascart and Bougeault, 2011) and in the most recent cycles of the global IFS model (ECMWF, 2012) the cloud SW inhomogeneity factor is set to 1.0. Some meteorological institutes also run hlradia (within the operational HIRLAM) with this setting. In the following cloud experiments (4–11) we set the cloud inhomogeneity factor to 1.0. In Sect. 4.2.3 we discuss the cloud SW inhomogeneity at a more general level.

The discrepancies between using the IFS radiation scheme with the HARMONIE 37h1 default cloud liquid optical property scheme (Fouquart, 1987), hlradia and the accurate
Figure 9. Global radiation as a function of cloud water load (experiment 4). The results from HS-DISORT (green dashed curve), IFS Fouquart with SW inhomogeneity factors of 0.7 (magenta dotted curve) and 1.0 (red curve), and hlradia with SW inhomogeneity factors of 0.8 (blue dashed curve) and 1.0 (black curve) are shown.

Table 3. Absolute differences (unit: W m$^{-2}$) for experiment 4. IFS-F refers to the IFS radiation scheme using the Fouquart (1987) liquid cloud optical property parameterisation. The numbers 0.7, 0.8 and 1.0 give the value of the cloud SW inhomogeneity factors.

<table>
<thead>
<tr>
<th>Cl. wat. [kg m$^{-2}$]</th>
<th>IFS-F 0.7 diff.</th>
<th>IFS-F 1.0 diff.</th>
<th>hlradia 0.8 diff.</th>
<th>hlradia 1.0 diff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>−3.05</td>
<td>−3.05</td>
<td>21.23</td>
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<td>0.001</td>
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<td>0.100</td>
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<td>23.76</td>
<td>32.22</td>
<td>−0.23</td>
</tr>
<tr>
<td>0.200</td>
<td>55.80</td>
<td>10.06</td>
<td>20.31</td>
<td>−3.79</td>
</tr>
<tr>
<td>0.500</td>
<td>23.34</td>
<td>−3.92</td>
<td>11.80</td>
<td>−0.97</td>
</tr>
<tr>
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<td>6.09</td>
<td>−8.05</td>
<td>7.86</td>
<td>0.78</td>
</tr>
<tr>
<td>2.000</td>
<td>−1.60</td>
<td>−7.72</td>
<td>5.25</td>
<td>1.52</td>
</tr>
<tr>
<td>5.000</td>
<td>−3.37</td>
<td>−4.41</td>
<td>3.05</td>
<td>1.51</td>
</tr>
</tbody>
</table>

Table 4. Absolute differences (unit: W m$^{-2}$) for experiment 4. IFS-F, IFS-S and IFS-N refer to the IFS radiation scheme using the Fouquart (1987), the Slingo (1989) and Nielsen liquid cloud optical property parameterisation, respectively.

<table>
<thead>
<tr>
<th>Cl. wat. [kg m$^{-2}$]</th>
<th>IFS-F diff.</th>
<th>IFS-S diff.</th>
<th>IFS-N diff.</th>
<th>hlradia diff.</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.000</td>
<td>−3.05</td>
<td>−3.05</td>
<td>−3.05</td>
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</tr>
<tr>
<td>0.001</td>
<td>9.22</td>
<td>2.93</td>
<td>5.06</td>
<td>29.39</td>
</tr>
<tr>
<td>0.002</td>
<td>10.47</td>
<td>0.18</td>
<td>3.79</td>
<td>41.01</td>
</tr>
<tr>
<td>0.005</td>
<td>18.12</td>
<td>−1.93</td>
<td>5.24</td>
<td>43.81</td>
</tr>
<tr>
<td>0.010</td>
<td>30.16</td>
<td>−1.54</td>
<td>9.86</td>
<td>44.99</td>
</tr>
<tr>
<td>0.020</td>
<td>41.10</td>
<td>−4.72</td>
<td>11.56</td>
<td>39.57</td>
</tr>
<tr>
<td>0.050</td>
<td>36.92</td>
<td>−20.93</td>
<td>−0.90</td>
<td>15.14</td>
</tr>
<tr>
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<td>23.76</td>
<td>−28.54</td>
<td>−10.53</td>
<td>−0.23</td>
</tr>
<tr>
<td>0.200</td>
<td>10.06</td>
<td>−23.71</td>
<td>−11.25</td>
<td>−3.79</td>
</tr>
<tr>
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<td>−5.23</td>
<td>−0.97</td>
</tr>
<tr>
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<td>−2.87</td>
<td>0.78</td>
</tr>
<tr>
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<td>−4.00</td>
<td>−2.15</td>
<td>1.52</td>
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<tr>
<td>5.000</td>
<td>−4.41</td>
<td>−1.32</td>
<td>−0.79</td>
<td>1.51</td>
</tr>
</tbody>
</table>

HS-DISORT model are shown in Fig. 10. In this figure the results obtained when using two alternative schemes are also shown. The first of these schemes is the Slingo (1989) scheme that is optionally available in HARMONIE 37h1, while the second is the Nielsen scheme as described by Eqs. (3)–(5) and Table 2. In Table 4 the results are shown in the form of absolute differences compared to the HS-DISORT calculations.

It can be seen that the default IFS radiation scheme in HARMONIE, with the Fouquart (1987) liquid cloud optical property scheme, shows a positive bias of up to +41 W m$^{-2}$ (+10 %) for clouds with a 0.02 kg m$^{-2}$ cloud water load but shows a smaller bias for more water-rich clouds. For the alternative Slingo (1989) scheme the results show a negative bias of up to −29 W m$^{-2}$ (−14 %) for clouds with a 0.1 kg m$^{-2}$ cloud water load. The Nielsen scheme has the lowest overall bias in this experiment, with a maximum bias of +12 W m$^{-2}$ (+3 %) for a cloud water load of 0.02 kg m$^{-2}$. There is a high positive bias of up to +45 W m$^{-2}$ (+10 %) for a cloud water load of 0.01 kg m$^{-2}$ for the hlradia scheme. For cloud water loads of 0.1 W m$^{-2}$ and higher, the hlradia scheme has practically no bias. Here the positive bias of the hlradia scheme in clear sky conditions (Figs. 1, 3, 4, 5 and 7) should be kept in mind. If this were to be corrected, the
hlradia results would be around 4% lower overall in this experiment.

In Figs. 11–14 the relative differences between the net fluxes as a function of height are shown for each of the four parameterisations tested. As for the global radiation, the net fluxes mostly have positive biases both below and above the clouds when the Fouquart parameterisation is used. An increasingly negative bias is seen below increasingly thicker clouds (Fig. 11). Also for the Slingo and Nielsen parameterisations increasingly negative biases are seen below increasingly thicker clouds. The results for the hlradia scheme do not display this pattern (Fig. 14). Instead, a clear negative bias ($< -20\%$) is seen in the net flux at the top of the thicker clouds, but not below and above these. Such a pattern can be explained by the cloud absorptance being too large and the cloud reflectance being too low in the hlradia scheme.

4.2.3 General discussion on cloud inhomogeneity

In an NWP model grid box clouds may be inhomogeneously distributed. It can easily be shown that representing clouds as a linear average covering a certain fraction of the grid box does not produce the same SW transmittance and reflectance as when the clouds are resolved. This is because the cloud transmittance and reflectance do not vary linearly with cloud optical depth. On the other hand, in cases where clouds are homogeneously distributed within a grid box the linear average is correct. Therefore, it is incorrect to multiply clouds in all grid boxes by the same cloud inhomogeneity factor, as is currently done in HARMONIE. To deal with these issues properly, and also to deal with the effects of 3-D cloud radiation transfer, a more sophisticated scheme like the one recently proposed by Hogan and Shonk (2013) is required.

4.2.4 Experiment 5: cloud drop effective radius

Experiment 5 was run to study the sensitivity of the schemes to varying $r_{e,liq}$, keeping the integrated cloud water load at 0.1 kg m$^{-2}$. The global radiation results are shown in Fig. 15 and in Tables 5 and 6. The net irradiance results relative to HS-DISORT are shown in Figs. 16–19.
The new Nielsen parameterisation clearly performs best compared to the HS-DISORT calculations (Fig. 15 and Tables 5–6). The Slingo parameterisation performs considerably worse when $r_{\text{e,liq}}$ is varied, which is in contrast to experiment 4 where the liquid cloud water load was varied (Fig. 10). This parameterisation was designed for a limited cloud droplet size range of 4.2–16.6 µm (Slingo, 1989). Therefore, it is not surprising that its performance deteriorates for large cloud droplet sizes. Previously, Dobbie et al. (1999) have shown that the Slingo parameterisation does not agree with calculations based on Mie theory for large cloud droplets. The Fouquart parameterisation has a consistently positive bias as a function of $r_{\text{e,liq}}$ relative to HS-DISORT. (+20 to +34 W m$^{-2}$ i.e. +8 to +22 %). The hlradia parameterisation performs very well for the small cloud droplets but has a positive bias for cloud droplets which are larger than 15 µm.

In Figs. 16–19 the corresponding results for the net flux differences are shown. Again, the bias in the net fluxes is consistently positive for all height levels when the Fouquart parameterisation is used (Fig. 16). The biases of the Slingo (Fig. 17) and Nielsen (Fig. 18) schemes are mainly below the cloud rather than above. For the Nielsen scheme the negative bias increases with decreasing $r_{\text{e,liq}}$. As in Fig. 15, the results for the hlradia scheme are also very good (Fig. 19) for the atmospheric net fluxes in this experiment.

### 4.2.5 Experiment 6 and 7: surface albedo under liquid cloud conditions

Experiment 6 was run for a fixed integrated cloud water load of 0.1 kg m$^{-2}$ and a fixed $r_{\text{e,liq}}$ of 10 µm. The results of varying the surface albedo can be seen in Fig. 20, which shows that the three cloud optical property parameterisations in the IFS scheme have similar sensitivities to surface albedo. The increase in global radiation as a function of surface albedo is less in the case of hlradia. When HS-DISORT is used the increase in global radiation as a function of the surface albedo is slightly larger than for each of the HARMONIE schemes.
Figure 16. As for Fig. 11 but for varying $r_{e, \text{liq}}$ (experiment 5). Relative differences in net fluxes between IFS-Fouquart and HS-DISORT.

Figure 17. As for Fig. 16 but for IFS-Slingo vs. HS-DISORT.

Figure 18. As for Fig. 16 but for IFS-Nielsen vs. HS-DISORT.

Figure 19. As for Fig. 16 but for hlradia vs. HS-DISORT.

4.3 Ice cloud experiments

Experiment 7 was run for a fixed integrated cloud water load of 1.0 kg m$^{-2}$ and was otherwise similar to experiment 6. As in experiment 6, it can be seen that the global radiation sensitivity in HS-DISORT as a function of the surface albedo is larger than for the HARMONIE cases (Fig. 21).

Four ice cloud experiments were run to test the SW radiation sensitivity to cloud ice load and cloud ice particle equivalent radius ($r_{e, \text{ice}}$) in the case of a typical land surface albedo of 0.18 and a typical snow surface albedo of 0.7. Experiments 8 and 9 were run for a fixed $r_{e, \text{ice}}$ of 50 µm. This is a typical value of $r_{e, \text{ice}}$ for pure ice clouds (Fu, 1996; Nielsen, 2011).
4.3.1 Experiments 8 and 9: cloud ice load

For the IFS radiation scheme, we tested the Fu and Liou (1993) ice cloud parameterisation, which is the default in Harmonie 37h1, and the more recent Fu (1996) parameterisation. As can be seen in Fig. 22, both of these parameterisations compare very well to the Fu-DISORT calculations in the cloud ice load sensitivity test with low albedo (experiment 8). In the high albedo case (experiment 9) both parameterisations show a significant negative bias for cloud ice loads of 0.2 kg m\(^{-2}\) and above as shown in Fig. 23. The hlradia scheme performs worse than the IFS schemes. Again, this can to a large extent be explained by the clear sky positive bias of hlradia. With the clear sky bias removed, the hlradia results in experiments 8 and 9 (Figs. 22 and 23) would be around 4% lower and much closer to the IFS scheme results. This also applies to experiments 10 and 11 (Figs. 24 and 25).

4.3.2 Experiments 10 and 11: cloud ice particle equivalent radius

In Figs. 24 and 25 the results from the two tests of SW sensitivity to \(r_{e,\text{ice}}\) are shown. It can be seen that the Fu (1996) parameterisation shows better agreement with the Fu-DISORT calculations than the Fu and Liou (1993) parameterisation. Both of these show a negative bias of approximately −10% for the smallest \(r_{e,\text{ice}}\) in the low and high surface albedo cases (Figs. 24 and 25).

In Figs. 26–28 the net flux differences relative to Fu-DISORT are shown for the Fu and Liou (1993) parameterisation, the Fu (1996) parameterisation and the hlradia scheme (Wyser et al., 1999), respectively. For the latter a strong positive bias is seen in the net fluxes at all atmospheric levels. In the two first cases the largest biases are seen under the clouds with the largest cloud ice loads. This is a similar pattern to that seen in the cloud liquid water load tests (Figs. 12 and 13).
In all parameterisations of cloud optical properties studied here, cloud ice was assumed to consist of hexagonal crystals. In reality, cloud ice particles come in multiple shapes (Baker and Lawson, 2006; Lawson et al., 2006). As shown by Kahnert et al. (2008), these shapes significantly affect the SW forcing of the cloud. Thus, the benchmarking quality of the Fu-DISORT run, in this case, is no better than the correctness of the basic assumption made on the cloud ice particle shape. It is only correct for ice clouds consisting of hexagonal crystals. In the libRadtran library it is possible to use alternative cloud ice particle shapes. Thus the DISORT runs could have been made for these. However, as all the cloud ice parameterisations in HARMONIE assume only hexagonal crystals, we have only performed tests for this cloud ice particle shape.

4.4 Discussion on the angular distribution of diffuse radiances

In the IFS scheme all scattered irradiance, including that transmitted diffusely through clouds, is modelled as having a zenith angle of 53.0°, i.e. the irradiance transmitted diffusely
through or reflected from clouds is assumed to be on average 60% (i.e. \( \cos(53.0^\circ) \)) of the irradiance normal to the surface (Mascart and Bougeault, 2011). An assumption like this is necessary in the delta-Eddington scheme or any scheme that does not resolve the angular distribution of the radiance (Thomas and Stamnes, 2002). In the 30-stream DISORT simulations the angular radiance distribution below clouds is resolved. Even for cases with conservative scattering the use of a fixed average solar zenith angle has been shown to be imprecise (Hopf, 1936; King, 1960; King et al., 1965). By comparing results of DISORT with results from the delta-Eddington radiative transfer scheme where both are given the exact same inherent optical properties as input, a direct test of the radiative transfer component of the HARMONIE IFS scheme can be made. We have included tests of several combinations of inherent optical properties in the Supplement Part 2.

In Fig. 29 a few of these test results are shown. These are for a single scattering albedo of 0.99, an asymmetry factor of 0.8 and a solar zenith angle of 53.0°. A non-reflecting surface is assumed. It can be seen that the IFS delta-Eddington scheme performs well for optical thicknesses of up to 0.5. An increasing positive bias is seen for higher optical thicknesses, peaking for \( \tau = 5 \) with a bias of +4%. For very high optical thicknesses, \( \tau > 50 \), large relative negative biases are seen; however, these are insignificant as can be seen in the upper plot of Fig. 29 because the absolute transmittance, and thereby the absolute error, is very low. In the supplement, it can be seen that this pattern of errors is similar also when the asymmetry factor and the solar zenith angle are varied.

The results of the delta-Eddington tests can now be compared with the previous results. First let us consider the cloud ice test results (experiment 8) shown in Figs. 22 and 27. In this experiment both DISORT and the IFS radiation scheme used the cloud optical property parameterisation of Fu (1996). Thus the differences must be partly due to the delta-Eddington approximation and partly due to the approximation of using a limited number of spectral bands. In the IFS scheme only five bands are used in practice as mentioned in Sect. 2.2. The maximum positive bias seen at a cloud ice load of 0.05 kg m\(^{-2}\) is similar to the one seen in Fig. 29. The increasingly negative biases, seen at increasing cloud ice loads, however, appear to be much more significant than those seen when testing the delta-Eddington scheme directly. These are thus likely to arise from the error made by using the five spectral bands. A similar conclusion can be drawn from studying the results when the IFS-Nielsen cloud liquid optical property parameterisation was used (Figs. 10 and 13).

The surface reflectance is also important for the angular distribution of the diffuse irradiances. In each of the experiments the surfaces were assumed to have angular distributions of scattering that follow Lambert’s cosine law

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**Figure 28.** As for Fig. 26 but for hlradia vs. Fu-DISORT

**Figure 29.** The results in this figure are calculated for an asymmetry factor \( g = 0.8 \) and a cosine solar zenith angle \( \mu_0 = 0.60 \). The upper plot shows comparison of DISORT and IFS transmittances for a single scattering albedo of 0.99 as a function of optical thickness \( \tau \). The lower plot shows the corresponding relative differences.
(Lambert, 1760). In reality, such surfaces do not exist (Lommel, 1889; Bhandari et al., 2011), but they are used in NWP and climate models due to the lack of computational resources needed to resolve the angular radiance distribution.

We suggest that implementing a variable average solar zenith angle for scattered irradiance could improve the radiative transfer calculations in the delta-Eddington scheme. This suggestion has previously been made by Thomas and Stamnes (2002).

5 Conclusions and outlook

Overall we have demonstrated an effective method for testing the radiative transfer computations performed in an NWP model. By defining simplified atmospheric and surface conditions in a single-column model, we have full control of the input and can make clean comparisons of the different parameterisations. Such baseline testing is a necessary first step towards studying the sensitivity of NWP model results to the radiation parameterisations, for which integration in time in a realistic evolving 3-D atmospheric environment is required.

We have found strengths and weaknesses of the IFS and hlradia parameterisations in HARMONIE in the controlled experiments and suggest the improvements outlined below.

Regarding the IFS SW radiation scheme with HARMONIE default settings in comparison to highly detailed radiative transfer calculations we found that:

- The clear sky computations show that IFS underestimates the atmospheric transmittance for the lowest water vapour loads.

- The Fu (1996) cloud ice optical property parameterisation compares better than the Fu and Liou (1993) parameterisation. However, both compare fairly well, given the assumption that cloud ice particles are hexagonal columns.

- A new optical property parameterisation for liquid clouds has been developed. We have shown that this is better than the parameterisations currently available in HARMONIE.

- Assuming climatological ozone profiles induces a SW error of a few percent at most.

Regarding the much simpler hlradia SW scheme which has only one SW spectral band we have found that:

- In the clear sky test cases a bias of +3 to +5% is found in most of the experiments.

- The cloud liquid transmittance formula currently used in hlradia performs impressively well, especially considering the simplicity of the hlradia parameterisation.

- The cloud ice transmittance calculated by hlradia is within 7% of that calculated by Fu-DISORT.

- Assuming a constant ozone SW absorptance induces an error of a few percent at most.

Based on the above we propose the following future work:

- The current choice of six spectral bands in HARMONIE/IFS should be re-assessed, as the first spectral band is irrelevant for NWP modelling.

- The effect of changing the SW cloud inhomogeneity factor from 0.7 (0.8) to 1.0 in all schemes should be tested against observations of global radiation in the framework of 3-D HARMONIE experiments.

- The effects on the general 3-D NWP results of using the Nielsen cloud liquid optical property parameterisation within the IFS scheme should be tested against observations of global radiation.

- In order to improve the delta-Eddington radiative transfer calculations, the possibility of using a variable average solar zenith angle for diffuse irradiances should be investigated.

- The hlradia gaseous transmission coefficients should be tuned to the Kato-DISORT clear sky results presented here and for the other AFGL atmospheric profiles.

- The impact of aerosols needs to be investigated.

The Supplement related to this article is available online at doi:10.5194/gmd-7-1433-2014-supplement.

Acknowledgements. We acknowledge the support of the International HIRLAM-B Programme, the radiative transfer library libRadtran, and those who contributed their work to this library.

Edited by: V. Grewe

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